

# **EXERCISE-01**

# **CHECK YOUR GRASP**

# SELECT THE CORRECT ALTERNATIVE (ONLY ONE CORRECT ANSWER)

<b>ELAS</b>	TIC	TTY	

1. Which one of the following substances possesses the highest elasticity:-

(A) Rubber

(B) Glass

(C) Steel

(D) Copper

2. The lower surface of a cube is fixed. On its upper surface, force is applied at an angle of 30 from its surface. The change will be in its:-

(A) Shape

(B) Size

(C) Volume

(D) Both shape and size.

3. A 2m long rod of radius 1 cm which is fixed from one end is given a twist of 0.8 radians. The shear strain developed will be :-

(A) 0.002

(B) 0.004

(C) 0.008

(D) 0.016

4. A force F is needed to break a copper wire having radius R. The force needed to break a copper wire of radius 2R will be :-

(A)  $\frac{F}{2}$ 

(B) 2F

(C) 4F

(D)  $\frac{F}{2}$ 

5. If the density of the material increase, the value of Young's modulus :-

(A) increases

(B) decreases

(C) first increases, then decreases

(D) first decreases, then increases

**6**. The following four wires are made of the same material. Which of these will have the largest extension when the same tension is applied-

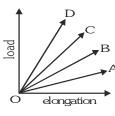
(A) Length 50 cm and diameter 0.5 mm

(B) Length 100 cm and diameter 1 mm

(C) Length 200 cm and diameter 2 mm

(D) Length 300 cm and diameter 3 mm

7. The load versus elongation graph for four wires of the same material and same length is shown in the figure. The thinnest wire is represented by the line



(A) OA

(B) OB

(C) OC

(D) OD

8X A fixed volume of iron is drawn into a wire of length  $\ell$  . The extension produced in this wire by a constant force F is proportional to :-

(A)  $\frac{1}{\ell^2}$ 

(B)  $\frac{1}{\ell}$ 

(C)  $\ell^2$ 

(D)  $\ell$ 

9. Two wires of the same material have lengths in the ratio 1:2 and their radii are in the ratio  $1:\sqrt{2}$ . If they are stretched by applying equal forces, the increase in their lengths will be in the ratio :-

(A) 2

(B)  $\sqrt{2}:2$ 

(C) 1 : 1

(D) 1 : 2

10× The area of cross-section of a wire of length 1.1 meter is 1 mm<sup>2</sup>. It is loaded with 1 kg. If Young's modulus of copper is  $1.1 ext{ } 10^{11} ext{ } N/m^2$ , then the increase in length will be (If g =  $10 ext{ } m/s^2$ ) :-

(A) 0.01 mm

(B) 0.075 mm

(C) 0.1 mm

(D) 0.15 mm

The Young's modulus of a rubber string 8 cm long and density 1.5 kg/m<sup>3</sup> is 5 10<sup>8</sup> N/m<sup>2</sup>, is suspended on the ceiling in a room. The increase in length due to its own weight will be :-

(A)  $9.6 10^{-5} m$ 

(B)  $9.6 10^{-11} m$ 

(C)  $9.6 10^{-3} m$ 

(D) 9.6 m

An increases in pressure required to decreases the 200 litres volume of a liquid by 0.004% in container is : (Bulk modulus of the liquid = 2100 MPa) :-

(A) 188 kPa

(B) 8.4 kPa

(C) 18.8 kPa

(D) 84 kPa

13. A ball falling in a lake of depth 200 m shows 0.1% decrease in its volume at the bottom. What is the bulk modulus of the material of the ball :-

(A) 19.6 10<sup>8</sup> N/m<sup>2</sup>

(B)  $19.6 10^{-10} N/m^2$  (C)  $19.6 10^{10} N/m^2$ 

(D)  $19.6 10^{-8} N/m^2$ 

Two wires of same diameter of the same material having the length  $\ell$  and  $2\ell$ . If the force F is applied on each, the ratio of the work done in the two wires will be :-

(A) 1 : 2

(B) 1:4

(C) 2 : 1

(D) 1:1

15. $\times$  A brass rod of cross-sectional area 1 cm<sup>2</sup> and length 0.2 m is compressed lengthwise by a weight of 5 kg. If Young's modulus of elasticity of brass is 1 10<sup>11</sup> N/m<sup>2</sup> and g = 10 m/sec<sup>2</sup>, then increase in the energy of the rod will be :-

(A)  $10^{-5}$  joule

(B) 2.5

 $10^{-5}$  joule (C) 5  $10^{-5}$  joule

(D)  $2.5 10^{-4}$  joule

16.X A weight is suspended from a long metal wire. If the wire suddenly breaks, its temperature :-

(A) Rises

(B) Falls

(C) Remains unchanged (D) Attains a value 0 K

# SURFACE TENSION

The length of needle floating on the surface of water is 1.5 cm. The force in addition to its weight required to lift the needle from water surface will be (surface tension of water = 7.5 N/cm) :-

(A) 22.5 N

(B) 2.25 N

(C) 0.25 N

The ring of radius 1m is lying on the surface of liquid. It is lifted from the liquid surface by a force of 4 Newtons in such a way that the liquid film in it remains intact. The surface tension of liquid will be :-

(A)  $\frac{1}{2\pi}$  N/m

(B)  $\frac{1}{\pi}$ N/m

(C)  $\frac{1}{3\pi}$  N/m (D)  $\frac{1}{4\pi}$  N/m

The radius of a soap bubble is r. The surface tension of soap solution is T. Keeping temperature constant, the radius of the soap bubble is doubled, the energy necessary for this will be :-

(A)  $24 \pi r^2 T$ 

(B)  $8 \pi r^2 T$ 

(C)  $12 \pi r^2 T$ 

(D)  $16 \pi r^2 T$ 

A liquid drop of diameter D breaks into 27 tiny drops. The resultant change in energy is :-

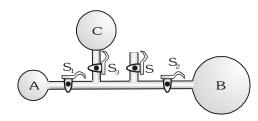
(A)  $2\pi$  TD<sup>2</sup>

(B)  $4\pi$  TD<sup>2</sup>

(C)  $\pi$  TD<sup>2</sup>

(D) None of these

The adjoining diagram shows three soap bubbles A, B and C prepared by blowing the capillary tube fitted with stop cocks S,  $S_1$ ,  $S_2$  and  $S_3$  with stop cock S closed and stop cocks  $S_1$ ,  $S_2$  and  $S_3$  opened :-



- (A) B will start collapsing with volumes of A and C increasing
- (B) C will start collapsing with volumes of A and B increasing
- (C) C and A will both start collapsing with the volume of B increasing
- (D) Volumes of A, B and C will become equal at equilibrium



22.	Pressures inside two soar (A) 102 : 101	p bubbles are 1.01 and 1 (B) $(102)^3 : (101)^3$	.02 atmospheres. Ratio be (C) 8 : 1	tween their volumes is :- (D) 2 : 1
23.				of water is $70  ext{ } 10^{-3}  ext{ Nm}^{-1}$ and in the pressure inside the bubble
	(A) 1.0270 10 <sup>5</sup> Pa	(B) 1.0160 10 <sup>5</sup> Pa	(C) 1.0144 10 <sup>5</sup> Pa	(D) 1.0131 10 <sup>5</sup> Pa
24.	Two soap bubbles each of (A) infinite	radius r are touching each (B) 2r	other. The radius of curvatur (C) r	e of the common surface will be: (D) $\mathrm{r}/2$
25.			d another soap bubble in v n, then the radius of the r (C) 5 cm	acuum has a radius of 4 cm. If new bubble is :- (D) 7 cm
26.	Shape of meniscus for a (A) Plane	liquid of zero angle of co (B) Parabolic	ntact is :- (C) Hemi-spherical	(D) Cylindrical
27.	If a water drop is kept b	etween two glass plates, t	hen its shape is :-	
	(A) (A)	(B)	(C)	(D) None the these
0.0	If	tube is dipped in water.	then water in it will –	
28.	(A) Rise up (C) Sometimes rise and s		(B) Depress (D) Rise up and come ou	ut as a fountain
29.	(A) Rise up (C) Sometimes rise and s	sometimes fall in a capillary at the surface	(D) Rise up and come ou	ut as a fountain
	<ul><li>(A) Rise up</li><li>(C) Sometimes rise and s</li><li>Water rises to a height h</li></ul>	sometimes fall in a capillary at the surface	(D) Rise up and come ou	
	<ul><li>(A) Rise up</li><li>(C) Sometimes rise and s</li><li>Water rises to a height h column in the same capil</li><li>(A) 6h</li><li>Two capillary tubes of same capillary t</li></ul>	sometimes fall  in a capillary at the surface llary will be :-  (B) $\frac{1}{6}$ h  me diameter are put vertica	(D) Rise up and come out of earth. On the surface of (C) h	of the moon the height of water
29.	<ul><li>(A) Rise up</li><li>(C) Sometimes rise and s</li><li>Water rises to a height h column in the same capil</li><li>(A) 6h</li><li>Two capillary tubes of same capillary t</li></ul>	sometimes fall  in a capillary at the surface llary will be :-  (B) $\frac{1}{6}$ h  me diameter are put vertica	(D) Rise up and come out of earth. On the surface of (C) h	of the moon the height of water  (D) zero  whose relative densities are 0.8
29.	<ul><li>(A) Rise up</li><li>(C) Sometimes rise and s</li><li>Water rises to a height h column in the same capil</li><li>(A) 6h</li><li>Two capillary tubes of san and 0.6 and surface tension</li></ul>	sometimes fall  in a capillary at the surface llary will be :-  (B) $\frac{1}{6}$ h  me diameter are put vertica	(D) Rise up and come out of earth. On the surface of (C) h	of the moon the height of water  (D) zero  whose relative densities are 0.8
29.	(A) Rise up (C) Sometimes rise and s  Water rises to a height h column in the same capit  (A) 6h  Two capillary tubes of sar and 0.6 and surface tension two tubes $\frac{h_1}{h_2}$ is :-  (A) $\frac{10}{9}$ In a capillary tube experi	sometimes fall  in a capillary at the surface llary will be :-  (B) $\frac{1}{6}$ h  me diameter are put vertications are 60 dyne/cm and $\frac{3}{10}$ ment, a vertical 30 cm lor capillary action. If this exp	(D) Rise up and come of earth. On the surface of earth. On the surface of (C) h  (C) h  (C) h  (C) $\frac{10}{3}$ (C) $\frac{10}{3}$	of the moon the height of water  (D) zero  whose relative densities are 0.8 Ratio of heights of liquids in the

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32. Water rises to a height of 16.3 cm in a capillary of height 18 cm above the water level. If the tube is cut at a height of 12 cm:-

- (A) Water will come as a fountain from the capillary tube
- (B) The height of the water in the capillary will be  $12\ \mathrm{cm}$
- (C) The height of the water in the capillary will be  $16.3\ cm$
- (D) Water will flow down in it's arms

- **33.** The height to which water rises in a capillary will be :-
  - (A) Maximum at 4 C
- (B) Maximum at 0 C
- (C) Minimum at 0 C
- (D) Minimum at 4 C
- **34.** Water rises in a capillary upto a height h. If now this capillary is tilted by an angle of 45, then the length of the water column in the capillary becomes:-
  - (A) 2h

(B)  $\frac{h}{2}$ 

- (C)  $\frac{h}{\sqrt{2}}$
- (D)  $h\sqrt{2}$
- **35.** If a capillary of radius r is dipped in water, the height of water that rises in it is h and its mass is M. If the radius of the capillary is doubled the mass of water that rises in the capillary will be :-
  - (A) 4M

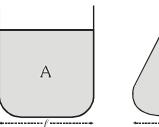
(B) 2M

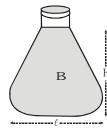
(C) M

- (D)  $\frac{M}{2}$
- **36.** Calculate the force required to separate the glass plate of area  $10^{-2}$  m $^2$  with a film of water 0.05 mm thick [surface tension of water is  $70 10^{-3}$  N/m] :-
  - (A) 25 N
- (B) 20 N
- (C) 14 N
- (D) 28 N
- 37. A vessel, whose bottom has round holes with diameter of 0.1 mm, is filled with water. The maximum height to which the water can be filled without leakage is :- (S.T. of water = 75 dyne/cm, g =  $1000 \text{ cm/s}^2$ )
  - (A) 100 cm
- (B) 75 cm
- (C) 50 cm
- (D) 30 cm

# **FLUID STATICS**

- **38**. A crown made of gold and copper weights 210 g in air and 198 g in water. The weight of gold in crown is:- [Given: Density of gold =  $19.3 \text{ g/cm}^3$  and Density of copper =  $8.5 \text{ g/cm}^3$ ]
  - (A) 93 g
- (B) 100 g
- (C) 150 g
- (D) 193 g
- **39**. To what height h should a cylindrical vessel of diameter d be filled with a liquid so that the total force on the vertical surface of the vessel be equal to the force on the bottom :-
  - (A) h = d
- (B) h = 2d
- (C) h = 3d
- (D) h = d/2
- **40.** Two vessels A and B have the same base area and contain water to the same height, but the mass of water in A is four times that in B. The ratio of the liquid thrust at the base of A to that at the base of B is :-





- (A) 4 : 1
- (B) 2:1
- (C) 1 : 1
- (D) 16:1
- **41.** Water stands upto a height h behind the vertical wall of a dam. What is the net horizontal force pushing the dam down by the stream, if width of the dam is  $\sigma$ ? ( $\rho$  = density of water):-
  - (A) 2hσg
- (B)  $\frac{h^2 \sigma \rho g}{2}$
- (C)  $\frac{h^2 \sigma \rho g}{4}$
- (D)  $\frac{h\sigma\rho g}{4}$
- 42. A U-tube is partially filled with water. Oil which does not mix with water is next poured into one side, until water rises by 25 cm on the other side. If the density of the oil is 0.8 g/cc, the oil level will stand higher than the water level by :-
  - (A) 6.25 cm
- (B) 12.50 cm
- (C) 18.75 cm
- (D) 25.00 cm



43.	The side of glass aquarium is the total force against (A) $980  ext{ } 10^3  ext{ N}$	_	ng. When the aquarium is to $(C) \ 0.98 \ 10^3 \ N$	filled to the top with water, what $ (D) \ 0.098  10^3 \ N $
44.		$\times~10^5~\text{N/m}^2$ must be main $50,000~\text{m}^3$ of water at a $\mu$ (B) $10^{10}~\text{J}$		pipes of a city. How much work $m^2$ – (D) $10^8\ J$
45.	then barometric height w	rill be :-		pectively. If it is taken to moon,
	(A) 76 mm	(B) 126.6 mm	(C) Zero	(D) 760 mm
46.	_	from the bottom of a lake n of water height H, then (B) 2H		doubles. If atmospheric pressure (D) 8H
47.		contained in a beaker. The upthrust on the body due		in figure
	(B) equal to weight of liq	uid displaced		
	(C) equal to weight of the (D) equal to the weight of	-		
48.	A boat having a length of a man gets on it. The m (A) 60 kg		etre is floating on a lake.  (C) 72 kg	The boat sinks by one cm when (D) 128 kg
49.	=	c. is immersed completely the body was 700g wt. Af (B) 800 g wt		ar. The weight of water and the vater and jar will be (D) 100 g wt
50.			_	/3part remains inside the water. ne piece of wood is to be drowned
	(A) 12 kg	(B) 10 kg	(C) 14 kg	(D) 15 kg
51.	<ul><li>(A) the density of metal i</li><li>(B) the density of metal i</li></ul>	s 3 g/cm³ s 7 g/cm³ times the density of the ui		ms in an unknown liquid. Then:—
52.	is 2 cm above water leve	l. The side of cube is :-	-	en the mass is removed the cube
	(A) 5 cm	(B) 10 cm	(C) 15 cm	(D) 20 cm
53.	A piece of ice with a stone (A) Increase	e frozen in it on water is kej (B) Decrease	pt in a beaker. The level of (C) Remain the same	water when ice completely melts— (D) None of these
54.	_	what change will occur in (B) It will rise	_	ith 5 cm side vertical. If it floats block.
55.		e 1000 cm³ is suspended fro f the block is below the su (B) 9 N		ght is 12 N in air. It is suspended ng of spring balance is :-

**67** 



- 56. A boat carrying a number of large stones is floating in a water tank. What will happen to the water level if the stones are unloaded into the water :-
  - (A) Rise
- (B) Fall
- (C) Remain unchanged
- (D) Rise till half the number of stones are unloaded and then begin to fall

### HYDRO DYNAMICS

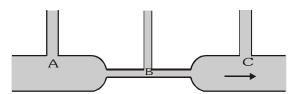
- Streamline motion is that motion in which there is:-
  - (A) Only longitudinal velocity gradient
- (B) Only radial velocity gradient
- (C) Longitudinal as well as radial velocity gradient (D) Neither longitudinal nor radial velocity gradient
- An aeroplane of mass 3 10<sup>4</sup> kg and total wing area of 120 m<sup>2</sup> is in a level flight at some height. The difference in pressure between the upper and lower surfaces of its wings in kilo pascal is  $(g=10 \text{m/s}^2)$ :
  - (A) 2.5

- (B) 5.0
- (C) 10.0
- (D) 12.5
- One end of a horizontal pipe is closed with the help of a valve and the reading of a barometer attached to the pipe is  $3 ext{ } 10^5$  pascal. When the value in the pipe is opened then the reading of barometer falls to 10<sup>5</sup> pascal. The velocity of water flowing through the pipe will be in m/s:-
  - (A) 0.2

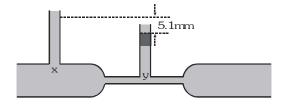
(B) 2

(C) 20

- (D) 200
- 16 cm $^3$  of water flows per second through a capillary tube of radius a cm and of length  $\ell$  cm when connected to a pressure head of h cm of water. If a tube of the same length and radius a/2 cm is connected to the same pressure head, the quantity of water flowing through the tube per second will be:-
  - (A) 16 cm<sup>3</sup>
- (B) 4cm<sup>3</sup>
- (C) 1 cm<sup>3</sup>
- A tank of height 5 m is full of water. There is a hole of cross sectional area 1 cm<sup>2</sup> in its bottom. The initial volume of water that will come out from this hole per second is :-
  - (A)  $10^{-3} \text{ m}^3/\text{s}$
- (B)  $10^{-4} \text{ m}^3/\text{s}$
- (C)  $10 \text{ m}^3/\text{s}$
- (D)  $10^{-2} \text{ m}^3/\text{s}$
- In the figure below is shown the flow of liquid through a horizontal pipe. Three tubes A, B and C are connected to the pipe. The radii of the tubes, A, B and C at the junction are respectively 2 cm, 1 cm. and 2 cm. It can be said that the :-



- (A) Height of the liquid in the tube A is maximum
- (B) Height of the liquid in the tubes A and B is the same
- (C) Height of the liquid in all the three tubes is the same
- (D) Height of the liquid in the tubes A and C is the same
- The diagram (figure) shows a venturimeter, through which water is flowing. The speed of water at X is 2 cm/s. The speed of water at Y (taking  $g = 1000 \text{ cm/s}^2$ ) is :-



- (A) 23 cm/s
- (B) 32 cm/s
- (C) 101 cm/s
- (D) 1024 cm/s
- Water contained in a tank flows through an orifice of a diameter 2 cm, under a constant pressure difference of 10 cm of water column. The rate of flow of water through the orifice is:-
  - (A) 44 cc/s
- (B) 4.4 cc/s
- (C) 444 cc/s
- (D) 4400 cc/s



### VISCOSITY

- 65. More viscous oil is used in summer than in winter in motors due to :-
  - (A) Rise in temperature in summer, the viscosity of oil decreases
  - (B) Rise in temperature in summer, viscosity of oil increases
  - (C) Surface tension of oil increases
  - (D) Surface tension of oil decreases
- **66**. With increase in temperature, the viscosity of :-
  - (A) Gases decreases and liquid increases
- (B) Gases increases and liquid decreases
- (C) Both gases and liquid increases
- (D) Both gases and liquid decreases
- 67. A rain drop of radius 0.3 mm has a terminal velocity in air 1m/s. The viscosity of air is  $18 ext{ } 10^{-5}$  poise. The viscous force on it is :-
  - (A) 101.73 10<sup>-4</sup> dyne

(B)  $101.73 10^{-5}$  dyne

(C)  $16.95 10^{-5}$  dyne

- (D)  $16.95 10^{-4} dyne$
- 68. Two liquids of densities  $d_1$  and  $d_2$  are flowing in identical capillaries under same pressure difference. If  $t_1$  and to are the time taken for the flow of equal quantities of liquids, then the ratio of coefficients of viscosities of liquids must be :-
- (B)  $\frac{d_1 t_1}{d_2 t_2}$
- (C)  $\frac{d_1 t_2}{d_2 t_1}$
- (D)  $\sqrt{\left(\frac{d_1t_1}{d_0t_0}\right)}$
- The velocity of falling rain drop attain limited value because of :-
  - (A) Surface tension

(B) Upthrust due to air

(C) Viscous force exerted by air

- (D) Air current
- 70. The rate of flow of liquid through a capillary tube, in an experiment to determine the viscosity of the liquid,
  - (A) When the pressure of the tube is increased
- (B) When the length of the tube is increased
- (C) When the radius of the tube is decreased
- (D) None of the above
- 71. A copper ball of radius 'r' travels with a uniform speed 'v' in a viscous fluid. If the ball is changed with another ball of radius '2r', then new uniform speed will be :-
  - (A) v

(B) 2v

(C) 4v

- (D) 8v
- Two drops of equal radius are falling through air with a steady velocity of 5cm/sec. If the two drops coalesce, then its terminal velocity will be :-

- (A)  $4^{\frac{1}{3}} \times 5 \text{ cm/s}$  (B)  $4^{\frac{1}{3}} \text{ cm/s}$  (C)  $5^{\frac{1}{3}} \times 4 \text{ cm/s}$  (D)  $4^{\frac{2}{3}} \times 5 \text{ cm/s}$

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Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Ans.	С	D	В	С	Α	Α	Α	С	С	С	В	D	Α	Α	В	Α	Α	В	Α	Α
Que.	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ans.	C	C	С	Α	C	C	C	В	Α	D	C	В	D	D	В	D	D	D	D	C
Que.	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans.	В	Α	В	В	С	С	Α	Α	В	Α	В	В	В	Α	D	В	Α	Α	С	С
Que.	61	62	63	64	65	66	67	68	69	70	71	72								
Ans.	Α	D	В	С	Α	В	Α	В	С	Α	С	Α								



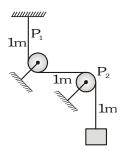
# **EXERCISE-02**

# **BRAIN TEASERS**

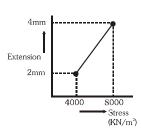
# Select the correct alternatives (one or more than one correct answers)

- 1. One end of uniform wire of length L and of weight W is attached rigidly to a point in the roof and a weight W is suspended from its lower end. If s is the area of cross-section of the wire, the stress in the wire at a height  $\frac{L}{4}$  from its lower end is :-

- (B)  $\left[ W_1 + \frac{W}{4} \right]$  (C)  $\left[ W_1 + \frac{3W}{4} \right]$  (D)  $\frac{W_1 + W}{4}$
- 2. A steel wire 1.5 m long and of radius 1 mm is attached with a load 3 kg at one end the other end of the wire is fixed it is whirled in a vertical circle with a frequency 2Hz. Find the elongation of the wire when the weight is at the lowest position-  $(Y = 2 10^{11} \text{ N/m} \text{ and } g = 10 \text{ m/s})$ 
  - (A) 1.77  $10^{-3} \text{ m}$
- (B)  $7.17 10^{-3} m$  (C)  $3.17 10^{-7} m$
- (D) 1.37 10<sup>-7</sup> m
- 3. A copper wire of length 3m and area of cross-section 1 mm<sup>2</sup>, passes through an arrangement of two frictionless pulleys,  $P_1$  and  $P_2$ . One end of the wire is rigidly clamped and a mass of 1 kg is hanged from the other end. If the Young's modulus for copper is  $10 10^{10} N/m^2$ , then the elongation in the wire is-



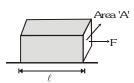
- (A) 0.05 mm
- (B) 0.1 mm
- (C) 0.2 mm
- (D) 0.3 mm
- 4. One end of a long metallic wire of length L area of cross section A and Young's modulus Y is tied to the ceiling. The other end is tied to a massless spring of force constant k. A mass m hangs freely from the free end of the spring. It is slightly pulled down and released. Its time period is given by-
  - (A)  $2\pi\sqrt{\frac{m}{1}}$
- (B)  $2\pi\sqrt{\frac{mYA}{kI}}$  (C)  $2\pi\sqrt{\frac{mk}{V\Delta}}$
- (D)  $2\pi\sqrt{\frac{m(kL + YA)}{kYA}}$
- 5. In determination of young modulus of elasticity of wire, a force is applied andextension is recorded. Initial length of wire is '1m'. The curve between extension and stress is depicted then Young modulus of wire will be:



- (A) 2  $10^9 \, \text{N/m}^2$
- (B) 1 109 N/m<sup>2</sup>
- $10^{10} \text{ N/m}^2$ (C) 2
- $10^{10} \text{ N/m}^2$ (D) 1

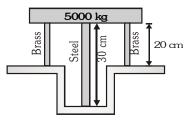


**6.** A block of mass 'M' area of cross-section 'A' & length ' $\ell$ ' is placed on smooth horizontal floor. A force 'F' is applied on the block as shown. If Y is young modulus of material, then total extension in the block will be:

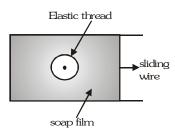


- (A)  $\frac{F\ell}{AY}$
- (B)  $\frac{F\ell}{2AY}$
- (C)  $\frac{F\ell}{3AY}$

- (D) cannot extend
- 7. A steel rod of cross-sectional area  $16~\text{cm}^2$  and two brass rods of cross section—area  $10~\text{cm}^2$  together support a load of 5000~kg as shown in figure. The stress in steel rod will be : (Take Y for steel =  $2.0~10^6~\text{N/cm}^2$ ) and for brass =  $1.0~10^6~\text{N/cm}^2$ )



- (A) 161.2 N/cm<sup>2</sup>
- (B) 151.4 N/cm<sup>2</sup>
- (C) 131.4 N/cm<sup>2</sup>
- (D) None of these
- **8.** The figure shows a soap film in which a closed elastic thread is lying. The film inside the thread is pricked. Now the sliding wire is moved out so that the surface area increases. The radius of the circle formed by elastic thread will:



- (A) increase
- (B) decreases
- (C) remains same
- (D) data insufficient
- 9. Water rise in a capillary upto a extension height such that upward force of surface tension balances the force of 75  $^{-10^{-4}}$  N due to weight of water. If surface tension of water is 6  $^{-10^{-2}}$  N/m. The internal circumference of the capillary must be :-
  - (A) 12.5 10<sup>-2</sup> m
- (B) 6.5 10<sup>-2</sup> m
- (C)  $0.5 10^{-2} \text{ m}$
- (D) 1.25 10<sup>-2</sup> n
- 10. In a U-tube diameter of two limbs are 0.5 cm and 1 cm respectively and tube has filled with water (T = 72 dyne/cm) then liquid level difference between two limbs will be :-
  - (A) 0.5 cm
- (B) 0.25 cm
- (C) 0.293 cm
- (D) none of these
- 11. On dipping a capillary of radius 'r' in water, water rises upto a height H and potential energy of water is  $u_1$ .

If a capillary of radius 2r is dipped in water, then the potential energy is  $u_2$ . The ratio  $\frac{u_1}{u_2}$  is :-

- (A) 2 : 1
- (B) 1:2
- (C) 4 : 1
- (D) 1:1
- 12. There are two thin films, A of liquid and B of polythene, identical in size. They are being pulled with same maximum weight W. If the breadth of the films is increased from b to 2b then the corresponding weights will be respectively
  - (A) W, W
- (B)  $\frac{W}{2}$ ,  $\frac{W}{2}$
- (C)  $\frac{W}{2}$ , W
- (D) W,  $\frac{W}{2}$



13. A capillary of the shape as shown is dipped in a liquid. Contact angle between the liquid and the capillary is 0 and effect to liquid inside the meniscus is to be neglected. T is surface tension of the liquid, r is radius of the meniscus, g is acceleration due to gravity and  $\rho$  is density of the liquid then height h in equilibrium is:

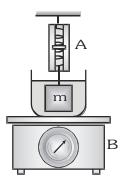


(A) Greater than  $\frac{2T}{r\rho g}$ 

(B) Equal to  $\frac{2T}{r\rho g}$ 

(C) Less than  $\frac{2T}{r\rho g}$ 

- (D) Of any value depending upon actual value
- 14. The spring balance A read 2 kg with a block m suspended from it. A balance B reads 5 kg when a beaker with liquid is put on the pan of the balance. The two balances are now so arranged that the hanging mass is inside the liquid in the beaker as shown in figure. In this situation:—

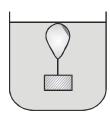


- (A) The balance A will read more than 2 kg
- (B) The balance B will read more than 5 kg
- (C) The balance A will read less than 2 kg and B will read more than 5 kg
- (D) The balance A and B will read 2 kg and 5 kg respectively.
- 15. A steel ball is floating in a trough of mercury. If we fill the empty part of the trough with water, what will happen to the steel ball :-
  - (A) It will continue in its position

(B) It will move up

(C) It will move down

- (D) It will execute vertical oscillations
- **16.** A balloon filled with air is weighted, so that it barely floats in water as shown in figure. When it is pushed down so that it gets submerged a short distance in water, then the balloon :-



- (A) Will come up again to its former position
- (B) Will remain in the position it is left

(C) Will sink to the bottom

- (D) Will emerge out of liquid
- 17. A wooden ball of density D is immersed in water of density d to a depth h below the surface of water upto which the ball will jump out of water is :-
  - (A)  $\frac{d}{D}h$
- (B)  $\left[\frac{d}{D}-1\right]h$
- (C) h

(D) zero



A solid uniform ball having volume V and density  $\rho$  floats at the interface of two unmixible liquids as shown in figure. The densities of the upper and the lower liquids are  $\rho_1$  and  $\rho_2$  respectively, such that  $\rho_1 < \rho < \rho_2$ . What fraction of the volume of the ball will be in the lower liquid :-

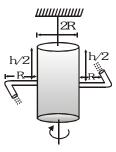


- (A)  $\frac{\rho \rho_2}{\rho_1 \rho_2}$

- **19**. A spherical ball of radius r and relative density 0.5 is floating in equilibrium in water with half of it immersed in water. The work done in pushing the ball down so that whole of it is just immersed in water is [p is the density of water] -
- (A) 0.25  $\rho$  rg (B) 0.5  $\rho$  rg (C)  $\frac{4}{3}\pi r^3 \rho g$ 
  - (D)  $\frac{5}{12} \pi r^4 \rho g$
- 20. The cylindrical tube of a spray pump has a radius R, one end of which has n fine holes, each of radius r. If the speed of flow of the liquid in the tube is v, the speed of ejection of the liquid through the hole is :-
  - (A)  $\frac{v}{n} \left[ \frac{R}{r} \right]$
- (B)  $\frac{v}{n} \left[ \frac{R}{r} \right]^{\frac{1}{2}}$  (C)  $\frac{v}{n} \left[ \frac{R}{r} \right]^{\frac{3}{2}}$
- (D)  $\frac{v}{n} \left\lceil \frac{R}{r} \right\rceil^2$
- 21. A cylindrical vessel filled with water is released on an inclined surface of angle  $\theta$  as shown in figure. The friction coefficient of surface with vessel is  $\mu(\le \tan \theta)$ . Then the constant angle made by the surface of water with the incline will be-

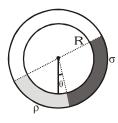


- (A)  $tan^{-1}\mu$
- (B)  $\theta \tan^{-1} u$
- (C)  $\theta$  + tan<sup>-1</sup>u
- (D) cot<sup>-1</sup>μ
- A cylindrical container of radius 'R' and height 'h' is completely filled with a liquid. Two horizontal L shaped pipes of small cross-section area 'a' are connected to the cylinder as shown in the figure. Now the two pipes are opened and fluid starts coming out of the pipes horizontally in opposite directions. Then the torque due to ejected liquid on the system is-

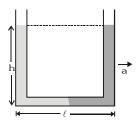


- (A) 4 aghpR
- (B) 8 aghpR
- (C) 2 aghpR
- (D) none of these

A small uniform tube is bent into a circular tube of radius R and kept in the vertical plane. Equal volumes of two liquids of densities  $\rho$  and  $\sigma$  ( $\rho > \sigma$ ) fill half of the tube as shown.  $\theta$  is the angle which the radius passing through the interface makes with the vertical. The value of  $\theta$  is :-



- (A)  $\theta = \tan^{-1} \left( \frac{\rho \sigma}{\rho + \sigma} \right)$  (B)  $\theta = \tan^{-1} \left( \frac{\sigma \rho}{\sigma + \rho} \right)$  (C)  $\theta = \tan^{-1} \left( \frac{\rho}{\rho + \sigma} \right)$  (D)  $\theta = \tan^{-1} \left( \frac{\rho}{\rho \sigma} \right)$
- A U-tube of base length ' $\ell$ ' filled with same volume of two liquids of densities  $\rho$  and  $2\rho$  is moving with an acceleration 'a' on the horizontal plane. If the height difference between the two surfaces (open to atmosphere) becomes zero, then the height h is given by-

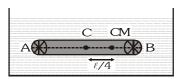


- (B)  $\frac{3a}{2g}\ell$

- (D)  $\frac{2a}{3q}\ell$
- A narrow tube completely filled with a liquid is lying on a series of cylinder as shown in figure. Assuming no sliding between any surfaces, the value of acceleration of the cylinders for which liquid will not come out of the tube from anywhere is given by



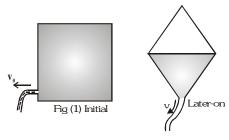
- (D)  $\frac{gH}{\sqrt{2}I}$
- A non uniform cylinder of mass m, length  $\ell$  and radius r is having its centre of mass at a distance  $\ell/4$  from the centre and lying on the axis of the cylinder. The cylinder is kept in a liquid of uniform density p, The moment of inertia of the rod about the centre of mass is I. The angular acceleration of point A relative to point B just after the rod is released from the position shown in figure is :



- (A)  $\frac{\pi \rho g \ell^2 r^2}{I}$



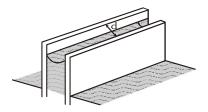
A square box of water has a small hole located in one of the bottom corner. When the box is full and sitting on a level surface, complete opening of the hole results in a flow of water with a speed  $\boldsymbol{v}_{\scriptscriptstyle 0}$ , as shown in figure (1). When the box is tilted by 45 and half filled so that the hole is at the lowest point. Now the water will flow out with a speed of:



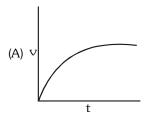
 $(A) v_0$ 

(B)  $\frac{v_0}{2}$ 

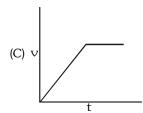
- (D)  $\frac{v_0}{\sqrt[4]{2}}$
- 28. Water filled in an empty tank of area 10 A through a tap of cross sectional area A. The speed of water flowing out of tap is given by v (m/s) =  $10 \left(1 - \sin \frac{\pi}{30} t\right)$  where 't' is in seconds. The height of water level from the bottom of the tank at t = 15 second will be:
  - (A) 10m
- (B)  $\left[15 + \frac{30}{\pi}\right]$  m (C)  $\frac{5}{4}$  m
- (D)  $\left[15 \frac{30}{\pi}\right]$  m
- Two very wide parallel glass plates are held vertically at a small separation d, and dipped in water. Some water climbs up in the gap between the plates. Let S be the surface tension of water,  $P_0$  = atmospheric pressure, P = pressure of water just below the water surface in the region between the plates-

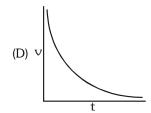


- (A)  $P=P_0 \frac{2S}{d}$  (B)  $P=P_0 + \frac{2S}{d}$
- (C)  $P=P_0 \frac{4S}{d}$
- (D)  $P=P_0 + \frac{4S}{d}$
- A piece of cork starts from rest at the bottom of a lake and floats up. Its velocity v is plotted against time t. Which of the following best represents the resulting curve-

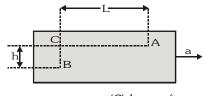


(B) v





A sealed tank containing a liquid of density  $\rho$  moves with a horizontal acceleration a, as shown in the figure. The difference in pressure between the points A and B is-

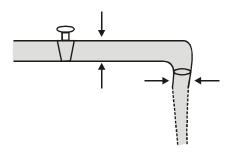


- (A) hpg
- (B) *ℓ*ρa

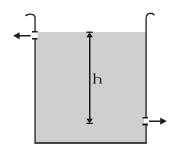
- (C) hρg lρa
- (D) hpg +  $\ell$ pa



- $\bf 32$ . The U-tube shown has a uniform cross-section. A liquid is filled in the two arms up to heights  $h_1$  and  $h_2$ , and then the liquid is allowed to move. Neglect viscosity and surface tension. When the levels equalize in the two arms, the liquid will-
  - (A) be at rest
  - (B) be moving with an acceleration of 9  $\left(\frac{h_1-h_2}{h_1+h_2+h}\right)$
  - (C) be moving with a velocity of  $(h_1-h_2)\ \sqrt{\frac{g}{2(h_1+h_2+h)}}$
  - (D) exert a net force to the right on the tube
- **33**. Water coming out of the mouth of a tap and falling vertically in streamline flow forms a tapering column, i.e., the area of cross-section of the liquid column decreases as it moves down. Which of the following is the most accurate explanation for this:-



- (A) As the water moves down, its speed increases and hence its pressure decreases. It is then compressed by the atmosphere.
- (B) Falling water tries to reach a terminal velocity and hence reduces the area of cross-section to balance upward and downward forces.
- (C) The mass of water flowing past any cross-section must remain constant. Also, water is almost incompressible. Hence, the rate of volume flow must remain constant. As this is equal to velocity area, the area decreases as velocity increases.
- (D) The surface tension causes the exposed surface area of the liquid to decrease continuously.
- **34**. There are two identical small holes on the opposite sides of a tank containing a liquid. The tank is open at the top. The difference in height between the two holes is h. As the liquid comes out of the two holes, the tank will experience a net horizontal force proportional to-



- (A)  $\sqrt{h}$
- (B) h

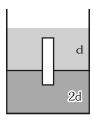
(C)  $h^{3/2}$ 

- (D) h<sup>2</sup>
- **35.** A U-tube of uniform cross-section is partially filled with a liquid I. Another liquid II which does not mix with liquid I is poured into one side. It is found that the liquid levels of the two sides of the tube are the same, while the level of liquid I has risen by 2 cm. If the specific gravity of liquid I is 1.1, the specific gravity of liquid II must be :-
  - (A) 1.12
- (B) 1.1
- (C) 1.05

(D) 1.0

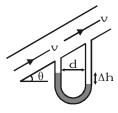


**36.** A homogeneous solid cylinder of length L (L < H/2), cross-sectional area A/5 is immersed such that it floats with its axis vertical at the liquid-liquid interface with length L/4 in the denser liquid as shown in the figure. The lower density liquid is open to atmosphere having pressure  $P_0$ . Then, density D of solid is given by :-

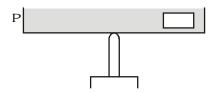


- (A)  $\frac{5}{4}$  d
- (B)  $\frac{4}{5}$  d
- (C) 4d

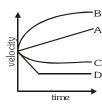
- (D)  $\frac{d}{5}$
- 37. A mercury manometer is connected as shown in the figure. The difference in height  $\Delta h$  is : (symbols have usual meaning).



- (A)  $\frac{\rho d \cot \theta}{\rho_{H\sigma}}$
- (B)  $\frac{\rho d \tan \theta}{\rho_{H\sigma}}$
- (C)  $\frac{\rho d \sin \theta}{\rho_{H\sigma}}$
- (D) None of these
- **38.** An open pan P filled with water (density  $\rho_{w}$ ) is placed on a vertical rod, maintaining equilibrium. A block of density  $\rho$  is placed on one side of the pan as shown. Water depth is more than height of the block.
  - (A) Equilibrium will be maintained only if  $\rho < \rho_w$
  - (B) Equilibrium will be maintained only  $\rho \leq \rho_{_{w}}$
  - (C) Equilibrium will be maintained for all relations between  $\rho$  and  $\rho_{_{W}}$
  - (D) Equilibrium will not be maintained in all cases.



39. A small ball is left in a viscous liquid form very much height. Correct graph of its velocity with time is :-



(A) A

(B) B

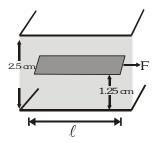
- (C) C
- (D) D
- **40.** A cubical block of side 'a' and density 'p' slides over a fixed inclined plane with constant velocity 'v'. There is a thin film of viscous fluid of thickness 't' between the plane and the block. Then the coefficient of viscosity of the thin film will be:



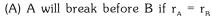
- (A)  $\frac{\rho agt \sin \theta}{U}$
- (B)  $\frac{\rho \operatorname{agt} \cos \theta}{V}$
- (C)  $\frac{v}{\rho \operatorname{agt} \sin \theta}$
- (D) None of these



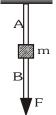
**41.** A space 2.5 cm wide between two large plane surfaces is filled with oil. Force required to drag a very thin plate of area  $0.5 \text{ m}^2$  just midway the surfaces at a speed of 0.5 m/s is 1N. The coefficient of viscosity in kg-sec/m<sup>2</sup> is:



- (A) 5 10<sup>-2</sup>
- (B)  $2.5 10^{-2}$
- (C)  $1 10^{-2}$
- (D) 7.5 10<sup>-2</sup>
- **42**. A large drop of oil, whose density is less than that of water, floats up through a column of water. Assume that the oil and the water do not mix. The coefficient of viscosity of the oil is  $\eta_{o}$  and that of water is  $\eta_{w}$ . The velocity of the drop will depend on-
  - (A) both  $\eta_o$  and  $\eta_w$
- (B)  $\eta_{0}$  only
- (C)  $\eta_{\scriptscriptstyle W}$  only
- (D) neither  $\eta_o$  nor  $\eta_w$
- 43. If the terminal speed of a sphere of gold (density =  $19.5 \text{ kg/m}^3$ ) is 0.2 m/s in a viscous liquid (density =  $1.5 \text{ kg/m}^3$ ), find the terminal speed of a sphere of silver (density =  $10.5 \text{ kg/m}^3$ ) of the same size in the same liquid.
  - (A) 0.4 m/s
- (B) 0.133 m/s
- (C) 0.1 m/s
- (D) 0.2 m/s
- $\textbf{44.} \quad \text{A spherical ball is dropped in a long column of viscous liquid.} \\ \quad \text{Which of the following graphs represent the variation of :-}$ 
  - (i) Gravitational force with time
  - (ii) Viscous force with time
  - (iii) Net force acting on the ball with time
  - (A) Q, R, P
- (B) R, Q, P
- (C) P, Q, R
- (D) R, P, Q
- **45.** A small sphere of mass m is dropped from a height. After it has fallen 100 m, it has attained its terminal velocity and continues to fall at that speed. The work done by air friction against the sphere during the first 100 m of fall is:
  - (A) Greater than the work done by air friction in the second 100 m
  - (B) Less tan the work done by air friction in the second 100 m
  - (C) Equal to 100 mg
  - (D) Greater than 100 mg
- **46**. The wires A and B shown in the figure are made of the same material, and have radii  $\,r_A$  and  $\,r_B$  respectively. The block between them has a mass m. When the force F is mg/3, one of the wires breaks-



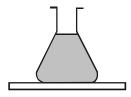
- (B) A will break before B if  $r_A < 2r_B$
- (C) Either A or B may break if  $r_A = 2r_B$
- (D) The lengths of A and B must be known to predict which wire will break



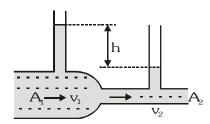
- **47**. When a capillary tube is dipped in a liquid, the liquid rises to a height h in the tube. The free liquid surface inside the tube is hemispherical in shape. The tube is now pushed down so that the height of the tube outside the liquid is less than h:-
  - (A) The liquid will come out of the tube like in a small fountain.
  - (B) The liquid will ooze out of the tube slowly.
  - (C) The liquid will fill the tube but not come out of its upper end.
  - (D) The free liquid surface inside the tube will not be hemispherical.



A massless conical flask filled with a liquid is kept on a table in a vacuum. The force exerted by the liquid on the base of the flask is  $W_1$ . The force exerted by the flask on the table is  $W_2$ .



- (C)  $W_1 \le W_2$
- (A)  $W_1 = W_2$  (B)  $W_1 > W_2$  (C)  $W_1 < W_2$  (D) The force exerted by the liquid on the walls of the flask is  $(W_1 W_2)$ .
- The vessel shown in the figure has two sections of areas of cross-section  $A_1$  and  $A_2$ . A liquid of density p fills both the sections, up to a height h in each. Neglect atmospheric pressure:-
  - (A) The pressure at the base of the vessel is 2hpg.
  - (B) The force exerted by the liquid on the base of the vessel is  $2h\rho gA_{2}$ .
  - (C) The weight of the liquid is  $\leq 2h\rho g A_2$ .
  - (D) The walls of the vessel at the level X exert a downward force hpg  $(A_2 A_1)$  on the liquid.
- 50. A liquid flows through a horizontal tube. The velocities of the liquid in the two sections, which have areas of cross–section  $A_1$  and  $A_2$ , are  $v_1$  and  $v_2$  respectively. The difference in the levels of the liquid in the two vertical tubes is h-



(A) The volume of the liquid flowing through the tube in unit time is  $A_1v_1$ 

(B) 
$$v_2 - v_1 = \sqrt{2gh}$$

- (C)  $v_2^2 v_1^2 = 2gh$
- (D) The energy per unit mass of the liquid is the same in both sections of the tube.
- A vertical U-tube contains a liquid. The total length of the liquid column inside the tube is  $\ell$ . When the liquid is in equilibrium, the liquid surface in one of the arms of the U-tube is pushed down slightly and released. The entire liquid column will undergo a periodic motion :-
  - (A) The motion is not simple harmonic motion.
  - (B) The motion is simple harmonic motion.
  - (C) If it undergoes simple harmonic motion, the time period will be  $2\pi\sqrt{\frac{\ell}{\sigma}}$
  - (D) It is undergoes simple harmonic motion, the time period will be  $2\pi\sqrt{\frac{\ell}{2\sigma}}$

BRAII	N TEASI	ERS				ANS	WER	KEY	7				EXI	ERCISE	-2
Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	В	Α	D	D	Α	В	Α	С	Α	С	D	D	С	С	В
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	С	В	С	D	D	Α	Α	Α	В	Α	В	D	D	Α	Α
Que.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans.	D	С	С	В	В	Α	В	В	С	Α	В	С	С	С	Α
Que.	46	47	48	49	50	51									
Ans.	A,B,C	C,D	В	A,B,C,D	A,C,D	B,D									

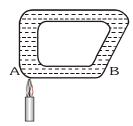


# **EXERCISE-03**

# **MISCELLANEOUS TYPE QUESTIONS**

# True/False

- 1. A big drop is formed by coalescing 1000 small droplets of water. The ratio of final surface energy to initial surface energy is 1/10.
- 2. Surface tension of antiseptics should be low.
- **3**. The blood pressure in humans is lower at the feet than at the brain.
- 4. If instead of fresh water, sea water is filled in a tank, then the velocity of efflux is changed.
- 5. If two row boats happen to sail parallel end close to each other, they experience a force which pulls then towards each other.
- **6**. A soda water bottle is falling freely, then the bubbles of the gas rise in the water of the bottle.
- 7. Water in a closed tube (see fig.) is heated with one arm vertically placed above a lamp. Water will begin to circulate along the tube in counter-clockwise direction.



Calaman II

**8.** A block of ice with a lead shot embedded in it is floating on water contained in a vessel. The temperature of the system is maintained at 0 C as the ice melts. When the ice melts completely the level of water in the vessel rises.

#### Fill in the blanks

- 1. Water is .....elastic than air.
- 2. Bulk modulus for an incompressible liquid is ......
- 3. A wire of length L and cross-sectional area A is made of a material of Young's modulus Y. If the wire is stretched by an amount x, the work done is .............

- **6.** With increase in temperature, viscosity of a liquid ......

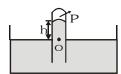
#### Match the Column

C-1...... I

1. Two soap bubbles coalesce to form a single large bubble.:

	Column 1		Column II
(A)	Surface energy in the process will	(p)	increase
(B)	Temperature of the bubble will	(q)	decrease
(C)	Pressure inside the soap bubble will	(r)	remains same

2. A tube is inverted in a mercury vessel as shown in figure. If pressure P is increased, then:



Column I

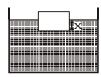
- (A) Height h
- (B) Pressure at O
- (C) Pressure at 1 cm above O

- Column II
- will increase
- (q) will decrease

(p)

(r) will remain same

3. A cube is floating in a liquid as shown in figure.



Column I

- (A) If density of liquid decreases then x will
- (B) If size of cube is increased then x will
- (C) If the whole system is accelerated

- Column II
- (p) increase
- (q) decrease
- (r) remains same upwards then x will
- **4**. A solid is immersed completely in a liquid. The coefficients of volume expansion of solid and the liquid are  $\gamma_1$  and  $\gamma_2$  ( $\langle \gamma_1 \rangle$ ). If temperatures of both are increased, then

Column I

- (A) Upthrust on the solid will
- (B) apparent weight of the solid will
- (C) Fraction of volume immersed in the

- Column II
- (p) increase
- (q) decrease
- (r) remains same liquid if allowed to float

#### Assertion & Reason

These questions contains, Statement 1 (assertion) and Statement II (reason).

1. **Statement-1**: A solid sphere and a hollow sphere of same material are floating in a liquid. Radius of both the spheres are same. Percentage of volume immersed of both the spheres will be same.

and

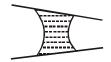
- Statement-2 : Upthrust acts on volume of liquid displaced. It has nothing to do whether the body is solid or hollow.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 2. Statement-1 : Upthrust on a solid block of iron when immersed in a lake will be less on the surface than on the bed of the lake.

and

- Statement-2 : On the surface of the lake density of water will be less than that at the bed and upthrust depends on the density of liquid.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true



 Statement-1: Two identical conical pipes shown in figure have a drop of water. The water drop tends to move towards tapered end.



and

- Statement-2 : Excess pressure is directed towards centre of curvature and inversely proportional to radius of curvature. Net excess pressure is therefore, directed towards tapered end. So the water drop tends to move towards tapered end.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 4. Statement-1: A ball allowed to swing in a region of uniform wind motion, will get an uplift.
  - Statement-2: Due to swing of the ball in a region of uniform wind motion, the difference in a velocity of air flow is present between the lower and upper position of ball, leading to varying pressure.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- Statement-1 : Elasticity restoring forces may be conservative.
   and
  - Statement-2 : The value of strain for same stress are different while increasing the load and while decreasing the load.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- Statement-1 : The bridges are declared unsafe after a long use.
   and
  - **Statement-2**: Elastic strength of bridges losses with time.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- 7. Statement-1: Young's modulus for a perfectly plastic body is zero.
  - **Statement-2**: For a perfectly plastic body, restoring force is zero.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- 8. Statement-1 : Identical springs of steel and copper are equally stretched. More work will be done on the steel spring.

and

**Statement-2**: Steel is more elastic than copper

- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true



9. Statement-1: The velocity of horizontal flow of a ideal liquid is smaller where pressure is large and vice versa.

and

- **Statement-2**: According to Barnoullis theorem for the stream line flow of an ideal liquid, the total energy per unit mass remains constant.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 10. Statement-1 : The shape of an automobile is so designed that its front resembles the stream line pattern of the fluid through which it moves.

and

- **Statement-2**: The shape of the automobile is made stream lined in order to reduce resistance offered by the fluid.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 11. Statement-1 : Machine parts are jammed in winter.

and

- Statement-2 : The viscosity of lubricant used in machine part decrease at low temperature.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 12. Statement-1 : The angle of contact of a liquid decrease with increase in temperature.

  and
  - Statement-2: With increase in temperature the surface tension of liquid increase.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- 13. Statement-1 : In gravity free space, the liquid in a capillary tube will rise to infinite height.

and

- Statement-2 : In the absence of gravity , there will be no force to prevent the rise of liquid due to surface tension.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 14. Statement-1 : It is better to wash the clothes in cold soap solution.
  - Statement-2 : The surface tension of cold solution is more than the surface tension of hot solution.:
    - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
    - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
    - (C) Statement-1 is true, Statement-2 is false
    - (D) Statement-1 is false, Statement-2 is true



 $\textbf{15. Statement-1} \quad : \text{ A gas filled balloon stops rising after it has attained a certain height in the sky}.$ 

and

- **Statement-2**: At the highest point, the density of air is such that the buoyant force on the balloon just equals its weight.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 16. Statement-1 : A parachute descends slowly whereas a stone dropped from same height falls rapidly.

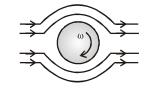
  and
  - Statement-2 : The viscous force of air on parachute is larger than that of on a falling stone.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- 17. Statement-1 : Hot soup tastes better than the cold soup.

and

- Statement-2 : Hot soup spread properly on our tongue due to lower surface tension.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 18. Statement-1: Roofs of buildings are blown off during a strong storm.

and

- **Statement-2**: Roofs of buildings becomes lighter during storm.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 19. Statement-1: The stream of water emerging from a water tap "necks down" as it falls.
  - Statement-2 : The volume flow rate at different levels is same.
  - (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
  - (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
  - (C) Statement-1 is true, Statement-2 is false
  - (D) Statement-1 is false, Statement-2 is true
- 20. Statement-1 : As wind flows left to right and a ball is spined as shown, there will be a lift of the ball.



#### and

- Statement-2 : Decrease in velocity of air below the ball, increases the pressure more than that above the ball.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true



21. Statement-1 : A block is immersed in a liquid inside a beaker, which is falling

freely. Buoyant force acting on block is zero.

and

Statement-2 : In case of freely falling liquid there is no pressure difference between any two points.



- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 22. Statement-1: An ice cube is floating in water in a vessel at  $0^{\circ}$ C. When ice cube melts, level of water in the vessel remain same.

and

Statement-2: Volume of melted ice is same as volume of water displaced by ice.

- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 23. Statement-1 : Leaves and small insects float on the surface of water buoyed up by Archimedes's principle.

  and

Statement-2 : They are not partially submerged. The objects are kept afloat by surface tension.

- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- **24**. **Statement-1**: Weight of a empty balloon measured in air is  $w_1$ . If air at atmospheric pressure is filled inside balloon and again weight of balloon is measured. Weight of balloon is  $w_2$  in second case. Then  $w_2$  is equal to  $w_1$ .

and

Statement-2 : Upthrust is equal to weight of the fluid displaced by the body.

- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 25. Statement-1 : The stretching of a coil is determined by its shear modulus. and

Statement-2 : Shear modulus change only shape of a body keeping its dimensions unchanged

- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- $\textbf{26. Statement-1} \quad \textbf{:} \quad \text{At critical temperature, surface tension of liquid becomes zero.}$

**Statement-2**: At this temperature, intermolecular forces for liquids and gases become equal. Liquid can expand without any restriction.

- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true



27. Statement-1: When a large soap bubble and a small soap bubble are connected by a capillary tube, the large bubble expands and while the small bubble shrinks.

and

- Statement-2 : The excess pressure inside a bubble is inversely proportional to radius.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 28. Statement-1 : The size of a hydrogen balloon increases as it rises in air.

and

- Statement-2: The material of the balloon can be easily stretched.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 29. Statement-1 : Smaller drops of liquid resist deforming forces better than the larger drops.

and

- **Statement-2**: Excess pressure inside a drop is directly proportional to its surface area.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 30. Statement-1 : Specific gravity of a fluid is a dimensionless quantity.

and

- Statement-2 : It is the ratio of density of fluid to the density of water.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 31. Statement-1: For Reynold number  $R_a > 2000$ , the flow of fluid is turbulent.

and

- Statement-2 : Inertial forces are dominant compared to the viscous forces at such high Reynold numbers.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true
- 32. Statement-1: A thin stainless steel needle can lay floating on a still water surface.

and

- Statement-2: Any object floats when the buoyancy force balances the weight of the object.
- (A) Statement-1 is true, Statement-2 is true; Statement-2 is correct explanation for Statement-1.
- (B) Statement-1 is true, Statement-2 is true; Statement-2 is NOT a correct explanation for Statement-1
- (C) Statement-1 is true, Statement-2 is false
- (D) Statement-1 is false, Statement-2 is true



# Comprehension Based questions

# Comprehension #1

If the container filled with liquid gets accelerated horizontally or vertically, pressure in liquid gets changed. In case of horizontally accelerated liquid  $(a_x)$ , the free surface has the slope  $\frac{a_x}{\sigma}$ . In case of vertically accelerated liquid (a) for calculation of pressure, effective g is used. A closed box with horizontal base 6m 6m and a height 2m is filled with liquid. It is given a constant horizontal acceleration g/2 and vertical downward acceleration  $\frac{g}{2}$ .

- 1. The angle of the free surface with the horizontal is equal to :
  - (A) 30

- (B)  $\tan^{-1} \frac{2}{3}$  (C)  $\tan^{-1} \frac{1}{3}$
- (D) 45

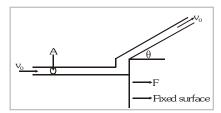
- Length of exposed portion of top of box is equal to: 2.

- (B) 3 m
- (C) 4 m
- (D) 2.5 m
- 3. Water pressure at the bottom of centre of box is equal to: (atmospheric pressure =  $10^5$  N/m<sup>2</sup>, density of water = 1000 kg/m<sup>3</sup>, g = 10 m/s<sup>2</sup>)
  - (A) 1.1 MPa
- (B) 0.11 MPa
- (C) 0.101 MPa
- (D) 0.011 MPa

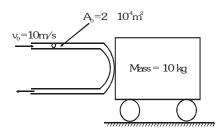
- 4. Maximum value of water pressure in the box is equal to:
  - (A) 1.4 MPa
- (B) 0.14 MPa
- (C) 0.104 MPa
- (D) 0.014 MPa
- 5. What is the value of vertical acceleration of box for given horizontal acceleration (g/2), so that no part of bottom of box is exposed:
  - (A)  $\frac{g}{2}$  upward
- (B)  $\frac{g}{4}$  downward (C)  $\frac{g}{4}$  upward (D) Not possible

# Comprehension #2

When jet of liquid strikes a fixed or moving surface, it exerts thrust on it due to rate of change of momentum.  $F = (\rho A v_0) v_0 - (\rho A v_0) v_0 \cos \theta = \rho A v_0^2 [1 - \cos \theta]$ 



If surface is free and starts moving due to thrust of liquid, then at any instant, the above equation gets modified based on relative change of momentum with respect to surface. Let any instant the velocity of surface is u, then above equation becomes -  $F = \rho A(v_0 - u)^2 [1-\cos \theta]$ 



Based on above concept, in the below given figure, if the cart is frictionless and free to move in horizontal direction, then answer the following : Given cross-section area of jet =  $2 mtext{10}^{-4} mtext{ m}^2$  velocity of jet  $mtext{v}_0 = 10 mtext{ m/s}$ , density of liquid =  $1000 \text{ kg/m}^3$ , Mass of cart M = 10 kg:



- 1. Initially (t = 0) the force on the cart is equal to :
  - (A) 20 N

- (B) 40 N
- (C) 80 N
- (D) zero

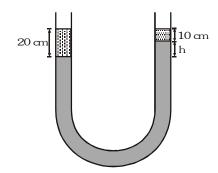
- **2.** Velocity of cart at t = 10 s. is equal to:
  - (A) 4 m/s

- (B) 6 m/s
- (C) 8 m/s
- (D) 5 m/s
- 3. In the above problem, what is the acceleration of cart at this instant -
  - (A)  $1.6 \text{ m/s}^2$
- (B)  $1 \text{ m/s}^2$
- (C)  $0.64 \text{ m/s}^2$
- (D)  $0.16 \text{ m/s}^2$
- 4. The time at which velocity of cart becomes 2m/s, is equal to:
  - (A) 1.6 s

- (B) 2 s
- (C) 3.2 s
- (D) 4s
- 5. The power supplied to the cart, when its velocity becomes 5 m/s, is equal to :
  - (A) 100 W
- (B) 25 W
- (C) 50 W
- (D) 200 W

# Comprehension #3

In a U-tube, if different liquids are filled then we can say that pressure at same level of same liquid is same.

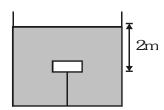


- 1. In a U-tube 20 cm of a liquid of density  $\rho$  is on left hand side and 10 cm of another liquid of density 1.5  $\rho$  is on right hand side. In between them there is a third liquid of density  $2\rho$ . What is the value of h.
  - (A) 5 cm

- (B) 2.5 cm
- (C) 2 cm
- (D) 7.5 cm
- 2. If small but equal lengths of liquid -1 and liquid -2 are increased in their corresponding sides then h will.
  - (A) remain same
- (B) increase
- (C) decrease
- (D) may increase or decrease

#### Comprehension #4

Newton's laws of motion can be applied to a block in liquid also. Force due to liquid (e.g., upthrust) are also considered in addition to other forces. A small block of weight W is kept inside. The block is attached with a string connected to the bottom of the vessel. Tension in the string is W/2.



- 1. The string is cut. Find the time when it reaches the surface of the liquid
  - (A)  $\frac{1}{\sqrt{5}}$  s
- (B)  $\sqrt{5}$  s
- (C)  $\sqrt{3}$  s
- (D)  $\frac{2}{\sqrt{5}}$  s
- 2. If weight of the block is doubled, then tension in the string becomes x times and the time calculated above becomes y times. Then
  - (A) x=2

(B)  $y = \sqrt{2}$ 

(C) both (A) and (B) are correct

(D) both (A) and (B) are wrong



# Comprehension #5

The human circulatory system can be thought of as a closed system of interconnecting pipes through which fluid is continuously circulated by two pumps. The two pumps, the right and left ventricles of the heart, work as simple two-stroke force pumps. The muscles of the heart regulate the force by contracting and relaxing. The contraction (systole) lasts about 0.2s, and a complete systole/diastole (contraction/relaxation) cycle lasts about 0.8 s.

For blood pressures and speeds in the normal range, the volume flow rate of blood through a blood vessel is directly proportional to the pressure difference over a length of the vessel and to the fourth power of the radius of the vessel.

The total mechanical energy per unit volume of blood just as it leaves the heart is : E/V =  $\rho gh$  + P +  $\rho v^2$ 

 ${f 1}$ . Why is diastolic blood pressure much lower than systolic pressure ?

(Note: A typical systole/diastole reading in mm Hg is 120/80)

- (A) Because the heart exerts more force on the blood during diastole
- (B) Because the heart exerts no force on the blood during diastole
- (C) Because the radii of the blood vessels increase during diastole, while the force exerted by the heart on the blood remains the same.
- (D) Because the radii of the blood vessels decrease during diastole, while the force exerted by the heart on the blood remains the same
- 2. Which of the following is a way to achieve approximately a 45% increase in the volume flow rate of blood through a blood vessel?
  - (A) Increase the radius by 10%
  - (B) Increase the cross-sectional area of the vessel by 10%
  - (C) Decrease the change in pressure by 10%
  - (D) Decrease the speed of flow by 10%
- 3. What is the gravitational potential energy of 8 cm<sup>3</sup> of blood in a 1.8 m tall man, in a blood vessel 0.3 m above his heart ? (**Note**: The man's blood pressure is  $1.3 ext{ } 10^4 ext{ } N/m^2$ .)
  - (A) 1 10<sup>-4</sup> J
- (B)  $2.5 10^{-2} J$
- (C)  $301 10^3 J$
- (D)  $4 10^4 J$
- **4**. The blood pressure in a capillary bed is essentially zero, allowing blood to flow extremely slowly through the tissues in order to maximize exchange of gases nutrients, and waste products. What is the work on 200 cm<sup>3</sup> of blood against gravity to bring it to the capillaries to the brain, 50 cm above the heart?
  - (A) 5145 J
- (B) 105 J
- (C) 10 J
- (D) 1 J
- 5. During intense exercise, the volume of blood pumped per second by an athlete's heart increases by a factor of 7, and his blood pressure increases by 20%/ By what factor does the power output of the heart increase during exercise?
  - (A) 1.2

(B) 3.5

(C) 7

(D) 8.4

# Comprehension #6

When an object moves through a fluid, as when a ball falls through air or a glass sphere falls through water, the fluid exerts a viscous force F on the object. This force tends to slow the object. For a small sphere of radius r, moving is given by Stoke's law,  $F_{\nu} = 6\pi\eta r\nu$ . In this formula,  $\eta$  is the coefficient of viscosity of the fluid, which is the proportionality constant that determines how much tangential force is required to move a fluid layer at a constant speed  $\nu$ , when the layer has an area A and is located a perpendicular distance z from and immobile surface. The magnitude of the force is given by  $F = \eta A\nu/z$ . For a viscous fluid to move from location 2 to location 1 along 2 must exceed that at location 1. Poiseuille's law gives the volume flow rate Q that results from such a pressure difference  $P_2 - P_1$ . The flow rate is

expressed by the formula :  $Q = \frac{\pi R^4 \left(P_2 - P_1\right)}{8 \eta L} \ \ Poiseuille's \ law \ remains \ valid \ as \ long \ as \ the \ fluid \ flow \ is \ laminar.$ 

For a sufficiently high speed, however, the flow becomes turbulent. Flow is laminar as long as the Reynolds number

is less than approximately 2000. This number is given by the formula  $:R_e=\frac{2\overline{\nu}\rho R}{\eta}$ . In which  $\overline{\nu}$  is the average speed,  $\rho$  is the density,  $\eta$  is the coefficient of viscosity of the fluid, and R is the radius of the pipe.



Take the density of water to be  $\rho = 1000 \text{ kg/m}^3$ .

- 1. Which of the following may be concluded from the information in the passage?
  - (A) The volume flow rate and the mass flow rate are the more for more viscous fluids
  - (B) The volume flow rate is smaller for more viscous fluids, whereas the mass flow rate is greater for more viscous fluids
  - (C) The volume flow rate is greater for more viscous fluids, whereas the mass flow rate is smaller for more viscous fluids
  - (D) The volume flow rate and the mass flow rate are greater for less viscous fluids
- 2. Blood vessel is 0.10 m in length and has a radius of  $1.5 10^{-3}$  m. Blood flows at rate of  $10^{-7}$  m $^3$ /s through this vessel. The pressure difference that must be maintained in this flow, between the two ends of the vessel, is 20 Pa. What is the viscosity sufficient of blood?
  - (A)  $2 10^{-3} \text{ Pa-s}$
- (B)  $1 10^{-3} Pa-s$
- (C)  $4 10^{-3} \text{ Pa-s}$
- (D) 5 10<sup>-4</sup> Pa-s
- 3. Calculate the highest average speed that blood ( $\rho \approx 1000 kg/m^3$ ) could have and still remain in laminar flow when it flows through the arorta (R= 8  $10^{-3}$ m). Take the coefficient of viscosity of blood to be  $4 10^{-3}$  Pa.s.
  - (A) 0.5 m/s
- (B) 1.0 m/s
- (C) 1.5 m/s
- (D) 2.0 m/s
- 4. What is the viscous force on a glass sphere of radius r=1mm falling through water ( $\eta=1$   $10^{-3}$  Pa-s) when the sphere has speed of 3m/s?
  - (A)  $2.7 10^{-2} N$
- (B) 2.5 10<sup>-5</sup> N
- (C)  $3.7 10^{-3} N$
- (D) 5.6 10<sup>-5</sup> N
- 5. If the sphere in previous question has mass of 1  $10^{-5}$  kg, what is its terminal velocity when falling through water ? ( $\eta = 1 \quad 10^{-3}$  Pa-s)
  - (A) 1.3 m/s
- (B) 3.4 m/s
- (C) 5.2 m/s
- (D) 6.5 m/s

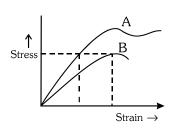
MIS	CELLANEOUS TYPE QUE	STION	ANS	SWER K	EY		EXERCISE -3
•	<u>True / False</u>	<b>1</b> . T	<b>2</b> . T	<b>3</b> . F	<b>4</b> . F <b>5</b> . T	6. F 7	. F <b>8</b> . F
•	Fill in the blanks:	1. More	2. Infinite	<b>3</b> . $\frac{1}{2}$	$\left(\frac{\text{YA}}{\text{L}}\right)$ x <sup>2</sup> <b>4</b> . $\frac{\text{Mg}}{3\text{AH}}$	<b>5</b> . 500	<b>6</b> . Decrease
•	Match the Column:	<b>1</b> . (A) q, (I	3) p, (C) q		2. (A) q, (B) r,	(C) r	
		<b>3</b> . (A) p, (	B) p, (C) r		<b>4</b> . (A) p, (B) q	, (C) q	
•	Assertion - Reason 9. A 10. A 11. C 22. A 23. D 24. A	12. C 13	3. A <b>14</b> . I	<b>15</b> . A		18. C 19.	A <b>20</b> . A <b>21</b> . A
•	Comprehension Bas	ed Quest	tions				
	Comprehension #1	: 1	. D	<b>2</b> . C	<b>3</b> . B	<b>4</b> . B	<b>5</b> . A
	Comprehension #2	: 1	. В	<b>2</b> . C	<b>3</b> . D	<b>4</b> . A	<b>5</b> . C
	Comprehension #3:	1	. В	<b>2</b> . C			
	Comprehension #4	: 1	. D.	<b>2</b> . A			
	Comprehension #5	: 1	. В	<b>2</b> . A	<b>3</b> . B	<b>4</b> . D	<b>5</b> . D
	Comprehension #6	: 1	. D	<b>2</b> . C	<b>3</b> . A	<b>4</b> . D	<b>5</b> . C

# EXERCISE-04 [A]

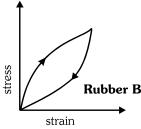
# **CONCEPTUAL SUBJECTIVE EXERCISE**

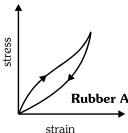
#### **ELASTICITY**

- The stress versus strain graphs for two materials A and B are shown. Explain
  - (i) Which material has greater Young's modulus?
  - (ii) Which material is more ductile?
  - (iii) Which material is more brittle?
  - (iv) Which of the two is the stronger material?

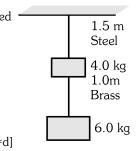


2. Two different types of rubber are found to have the stress-strain curves as shown in figure.





- (i) A heavy machine is to be installed in a factory. To absorb vibrations of the machine, a block of rubber is placed between the machinery and the floor. Which of the two rubbers A and B would you prefer to use for this purpose ? Why ?
- (ii) Which of the two rubber materials would you choose for a car tyre?
- 3. The maximum stress that can be applied to the material of a wire used to suspend an elevator is  $\frac{3}{\pi}$   $10^8$  N/m². If the mass of elevator is 900 kg and it move up with an acceleration 2.2 m/s² than calculate the minimum radius of the wire..
- Two wires of diameter 0.25 cm, one made of steel and other made of brass are loaded as shown in figure. The unloaded length of steel wire is 1.5 m and that of brass wire is 1.0 m. Young's modulus of steel is  $2.0 10^{11}$  Pa and that of brass is  $0.91 10^{11}$  Pa. Calculate the elongation of steel and brass wires. (1 Pa = 1 Nm<sup>-2</sup>)

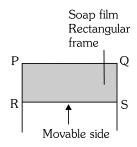


- $\textbf{5}. \hspace{0.5cm} \textbf{A steel rope has length $L$, area of cross-section $A$, Young's modulus $Y$. [Density =d]}\\$ 
  - (i) It is pulled on a horizontal frictionless floor with a constant horizontal force F = [dALg]/2 applied at one end. Find the strain at the midpoint.
  - (ii) If the steel rope is vertical and moving with the force acting vertically up at the upper end. Find the strain at distance L/3 from lower end.
- 6. If a compressive force of  $3.0 10^4\, N$  is exerted on the end of a  $20\, cm$  long bone of cross-sectional area  $3.6\, cm^2$ . (i) Will the bone break and (ii) if not, by how much length does it shorten? Given compressive strength of bone =  $7.7 10^8\, N/m^2$  and young's modulus of bone =  $1.5 10^{10}\, N/m^2$ .
- 7. A light rod of length 2m is suspended from the ceiling horizontally by means of two vertical wires of equal length tied to its ends. One of the wires is made of steel and is of cross-sectional area 0.1sq. cm and the other is of brass of cross-sectional area 0.2 sq. cm. Find out the position along the rod at which a weight may be hung to produce equal stresses in both wires. : Y for steel =  $20 ext{ } 10^{11}$  dyne cm<sup>-2</sup> and Y for brass =  $10 ext{ } 10^{11}$  dyne m<sup>-2</sup>.

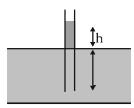
# SURFACE TENSION

8. PQRS is a rectangular frame of copper wire shown in figure the side RS of the frame is movable. If a soap film is formed on it then what is the diameter of the wire to maintain equilibrium (Given surface tension of soap solution = 0.045 N/m and density of copper =  $8.96 \cdot 10^3 \text{ kg/m}^3$ )





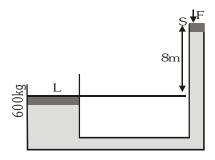
- 9. The pressure of air in a soap bubble of 0.7 cm diameter is 8 mm of water above the atmospheric pressure. Calculate the surface tension of soap solution. (Take  $g = 980 \text{ cm/sec}^2$ )
- 10. Two soap bubbles whose radii are  $R_1$  and  $R_2$  coalesce to form a new bubble (Isothermally). Whose radius is R. If change in volume of air inside bubble is V and change in area of whole surface is S, then show that 3PV + 4ST = 0 where P is the atmospheric pressure and T is the surface tension of the soap solution.
- 11. The capillary tube is dipped in water vertically. It is sufficiently long so that water rises to maximum height h in the tube. The length of the portion immersed in water is  $\ell > h$ . The lower end of the tube is closed, the tube is taken out and opened again. Then, find the length of the water column remaining in the tube.



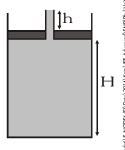
12. There is soap bubble of radius  $2.4 10^{-4}$  m in air cylinder which is originally at the pressure of  $10^5 \text{ N/m}^2$ . The air in the cylinder is now compressed isothermally until the radius of the bubble is halved. Calculate now the pressure of air in the cylinder. The surface tension of the soap film is  $0.08 \text{ Nm}^{-1}$ .

### **FLUID STATICS**

- 13. A hydraulic automobile lift is designed to lift cars with a maximum mass of 3000 kg. The area of cross-section of the piston carrying the load is  $425 \text{ cm}^2$ . What maximum pressure would the piston have to bear? (taking  $g = 10 \text{ m/s}^2$ )
- 14. For the system shown in the figure, the cylinder on the left at L has a mass of 600 kg and a cross sectional area of 800 cm<sup>2</sup>. The piston on the right, at S, has cross sectional area 25 cm<sup>2</sup> and negligible weight. If the apparatus is filled with oil ( $\rho = 0.75$  gm/cm<sup>3</sup>) Find the force F required to hold the system in equilibrium.

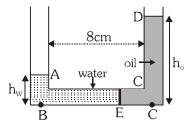


15. A piston of mass M=3kg and radius R=4cm has a hole into which a thin pipe of radius r= 1cm is inserted. The piston can enter a cylinder tightly and without friction, and initially it is at the bottom of the cylinder. 750 gm of water is now poured into the pipe so that the piston & pipe are lifted up as shown. Find the height H of water in the cylinder and height h of water in the pipe.

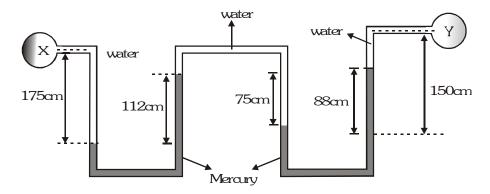




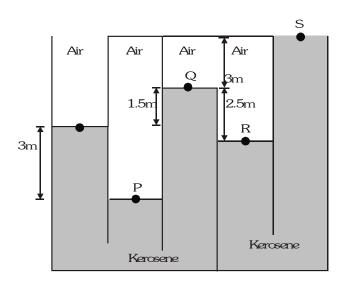
- **16**. An air bubble doubles its volume as it rises from the bottom of a tank to its surface. If the atmospheric pressure be 76 cm of Hg, what is the depth of the tank?
- 17. Two identical cylindrical vessels with their bases at the same level each contain a liquid of density  $\rho$ . The height of the liquid in one vessel is  $h_1$  and in the other is  $h_2$ . The area of either base is A. What is the work done by gravity in equalising the levels when the two vessels are connected?
- 18. A tube of uniform cross-section has two vertical portions connected with a horizontal thin tube 8 cm long at their lower ends. Enough water to occupy 22 cm of the tube is poured into one branch and enough oil of specific gravity 0.8 to occupy 22 cm is poured into the other. Find the position of the common surface E of the two liquids.



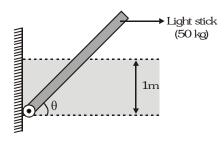
19. Two U-tube manometers are connected in series as shown in figure. Determine difference of pressure between X and Y. Take specific gravity of mercury as 13.6



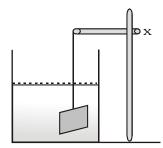
20. The container shown below holds kerosene and air as indicated. Compute the pressure at P, Q, R and S in  $KN/m^2$ . Take specific gravity of kerosene as 0.8



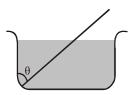
21. A light metal stick of square cross-section (5 cm 5cm) and length '4m' mass 2.5 kg and is shown in the figure below. Determine its angle of inclination when the water surface is 1m above the hinge. What minimum depth of water above high will be required to bring the metal stick in vertical position.



**22**. A metallic plate having shape of a square is suspended as shown in figure. The plate is made to dip in water such that level of water is well above that of the plate. The point 'x' is then slowly raised at constant velocity. Sketch the variation of tension T in string with the displacement 'S' of point x.



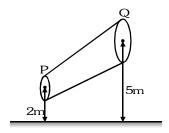
- 23. A block weight 15 N in air and 12 N when immersed in water. Find the specific gravity of block.
- **24.** A wooden plank of length 1m and uniform cross-section is hinged at one end to the bottom of a tank as shown in figure. The tank is filled with water upto a height 0.5 m. The specific gravity of the plank is 0.5. Find the angle  $\theta$  that the plank makes with the vertical in the equilibrium position. (exclude the  $\cos\theta=0$ ).



25. A glass beaker is placed partially filled with water in a sink. It has a mass of 390 gm and an interior volume of 500 cm<sup>3</sup>. When water starts filling the sink, it is found that if beaker is less than half full it will float. But if it is more than half full, it remains on the bottom of the sink, as the water rises to its rim. What is the density of the material of which the beaker is made?

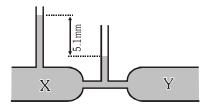
#### FLUID DYNAMICS

**26.** A non-viscous liquid of constant density  $1000 \text{ kg/m}^3$  flows in streamline motion along a tube of variable cross-section. The tube is kept inclined in the vertical plane as shown in the figure. The area of cross-section of the tube at two points P and Q at height of 2 m and 5m metres are respectively 4  $10^{-3} \text{ m}^2$  and 8  $10^{-3} \text{ m}^2$ . The velocity of the liquid at point P is 1 m/s. Find the work done per unit volume by the pressure and the gravity forces as the fluid flows from point P to Q.

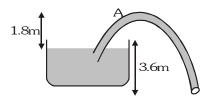




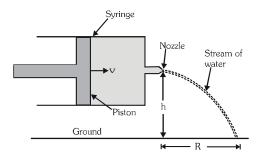
- 27. A large open top container of negligible mass and uniform cross–sectional area A has a small holes of cross–sectional area  $\frac{A}{100}$  in its side wall near the bottom. The container contains a liquid of density  $\rho$  and mass
  - $m_n$ . Assuming that the liquid starts flowing out horizontally through the hole at t = 0. Calculate:
  - (i) the acceleration of the container and
  - (ii) its velocity when 75% of the liquid has drained out.
- **28.** The diagram shows venturimeter through which water is flowing. The speed of water at X is 2 cm/sec. Find the speed of water at Y (taking  $g = 1000 \text{ cm/sec}^2$ ).



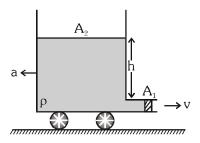
**29**. A siphon has a uniform circular base of diameter  $\frac{8}{\sqrt{\pi}}$  cm with its crest A 1.8 m above water level as in figure. Find (i) velocity of flow (ii) discharge rate of the flow in m³/sec (iii) absolute pressure at the crest level A. [Use  $P_0 = 10^5 \text{ N/m}^2 \& g = 10 \text{ m/s}^2$ ]



**30**. A syringe containing water is held horizontally with its nozzle at a height h above the ground as shown in fig. The cross-sectional areas of the piston and the nozzle are A and a respectively. The piston is pushed with a constant speed v. Find the horizontal range R of the stream of water on the ground.



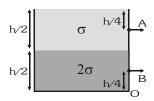
**31.** In a movable container shown in figure a liquid of density  $\rho$  is filled—up to a height h. The upper & lower tube cross sectional areas are  $A_2$  &  $A_1$  respectively ( $A_2 >> A_1$ ). If the liquid leaves out the container through the tube of cross-sectional area  $A_1$  then find –



- (i) Velocity of liquid coming out.
- (ii) Backward acceleration of the container.



A large tank is filled with two liquids of specific gravities  $2\sigma$  and  $\sigma$ . Two holes are made on the wall of the tank as shown. Find the ratio of the distance from O of the points on the ground where the jets from holes A & B strike.



# **VISCOSITY**

- A flask contains glycerine and the other contains water. Both are stirred vigorously and placed on the table. In which flask will the liquid come to rest earlier and why?
- There is a 1mm thick layer of glycerine between a flat plate of area 100 cm<sup>2</sup> and a big plate. If the coefficient of viscosity of glycerine is 1.0 kg/m-sec, then how much force is required to move the plate with a velocity of 7 cm/sec.
- 35. A spherical ball of radius 3  $10^{-4}$  m and density  $10^4$  kg/m<sup>3</sup> falls freely under gravity through a distance h before entering a tank of water. If after entering the water the velocity of the ball does not change, find h. The viscosity of water is  $9.8 10^{-6} N-s/m^2$ .

#### CONCEPTUAL SUBJECTIVE EXERCISE

# ANSWER KEY

EXERCISE-4(A)

- 1. (i) A (ii) A (iii) B (iv) A
- 2. (i) B (ii) A
- **3**. 6 mm
- **4.** Steel wire : 1.49  $10^{-4}$ m, Brass wire : 1.31  $10^{-4}$  m **5.** (i)  $\frac{dgL}{4Y}$  (ii)  $\frac{dgL}{6Y}$  **6.** (i) No (ii) 1.11 mm

- 7.  $\frac{4}{3}$  m from steel wire 8. 1.14 mm
- 9. 68.6 dyne/cm0<sup>5</sup> Pa14. 37.5 N
  - **11**. 2h

- **12**. 8.08 10<sup>5</sup> N/m<sup>2</sup> **13**. 7.06 10<sup>5</sup> Pa
- **15.**  $H = \frac{11}{32\pi} m$ ,  $h = \frac{2}{\pi} m$  **16.** 10.34 m **17.**  $-A \rho g \left[ \frac{h_1 h_2}{2} \right]^2$  **18.** BE = 6 cm

- **19.** 248 kN/m<sup>2</sup> **20.**  $P_p=124.9$  kN/m<sup>2</sup>,  $P_Q=89.5$  kN/m<sup>2</sup>,  $P_R=89.5$  kN/m<sup>2</sup>,  $P_S=46.4$  kN/m<sup>2</sup> **21.**  $\theta=30^{\circ}$  depth of water  $\geq 2m$  **22.** T **23. 24.**  $45^{\circ}$  **25.** 2.78

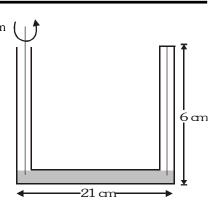
**29**. (i)  $6\sqrt{2}$  m/s, (ii)  $9.6\sqrt{2}$   $10^{-3}$  m<sup>3</sup>/s (iii) 4.6  $10^4$  N/m<sup>2</sup>

- **31**. (i)  $v = (\sqrt{2gh})$  (ii)  $a = \frac{2gA_1}{A_2}$  **32**.  $\sqrt{3} : \sqrt{2}$  **33**. Glycerine Flask **34**. 0.7 N

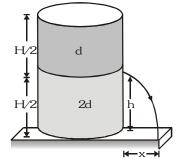
- **35**. 1.65 10<sup>3</sup> m

# **BRAIN STORMING SUBJECTIVE EXERCISE**

1. Length of horizontal arm of a uniform cross-section U-tube is  $\ell=21$  cm and ends of both of the vertical arms are open to surrounding of pressure  $10500~N/m^2.$  A liquid of density  $\rho=10^3~kg/m^3$  is poured into the tube such that liquid just fills the horizontal part of the tube. Now one of the open ends is sealed and the tube is then rotated about a vertical axis passing through the other vertical arm with angular velocity  $\omega_0=10~{\rm rad/s}.$  If length of each vertical arm be a = 6 cm. Calculate the length of air column in the sealed arm : [g=10m/s²]



- 2. A ball of density d is dropped on to a horizontal solid surface. It bounces elastically from the surface and returns to its original position in a time  $t_1$ . Next, the ball is released and it falls through the same height before striking the surface of a liquid of density  $d_1$ .
  - (i) If  $d \leq d_L$ , obtain an expression (in terms of d,  $t_1$  and  $d_L$ ) for the time  $t_2$  the ball takes to come back to the position from which it was released.
  - (ii) is the motion of the ball simple harmonic?
  - (iii) If  $d = d_L$ , how does the speed of the ball depend on its depth inside the liquid? Neglect all frictional and other dissipative forces. Assume the depth of the liquid to be large.
- 3. A container of large uniform cross-sectional area A resting on a horizontal surface, holds two immiscible, non-viscous and incompressible liquids of densities d and 2d, each of height  $\frac{H}{2}$  as shown in figure. The lower density liquid is open to the atmosphere having pressure  $P_0$ .



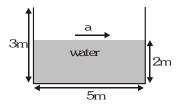
(i) A homogeneous solid cylinder of length  $L\left(L < \frac{H}{2}\right)$ , cross-

sectional area  $\frac{A}{5}$  is immersed such that if floats with its axis vertical at the liquid-liquid interface with length  $\frac{L}{4}$  in the denser liquid. Determine:

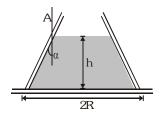
- (a) the density D of the solid, (b) the total pressure at the bottom of the container.
- (ii) The cylinder is removed and the original arrangement is restored. A tiny hole of area s (s<<A) is punched on the vertical side of the container at a height h  $\left(h < \frac{H}{2}\right)$ . Determine :
  - (a) the initial speed of efflux of the liquid at the hole
  - (b) the horizontal distance x travelled by the liquid initially, and
  - (c) the height  $h_m$  at which the hole should be punched so that the liquid travels the maximum distance  $x_m$  initially. Also calculate  $x_m$ . (Neglect the air resistance in these calculations)
- 4. A solid block of volume V =  $10^{-3}$  m³ and density d = 800 kg/m³ is tied to one end of a string, the other end of which is tied to the bottom of the vessel. The vessel contains 2 immiscible liquids of densities  $\rho_1 = 1000$  kg/m³ and  $\rho_2 = 1500$  kg/m³. The solid block is immersed with 2/5th of its volume in the liquid of higher density & 3/5th in the liquid of lower density. The vessel is placed in an elevator which is moving up with an acceleration of a =g/2. Find the tension in the string. [g = 10 m/s²]



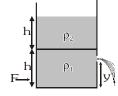
**5**. An open rectangular tank 5 m x 4m x 3m high containing water upto a height of 2m is accelerated horizontally along the longer side.



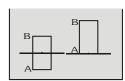
- (i) Determine the maximum acceleration that can be given without spilling the water.
- (ii) Calculate the percentage of water split over, if this acceleration is increased by 20%.
- (iii) If initially, the tank is closed at the top and is accelerated horizontally by 9m/s², find the gauge pressure at the bottom of the front and rear walls of the tank.
- **6**. A ship sailing from sea into a river sinks X mm and on discharging the cargo rises Y mm. On proceeding again into sea the ship rises the Z mm. Find the specific gravity of sea-water assuming the faces of ship are vertically along the line of sea-water.
- 7. A conical vessel without a bottom stands on a table. A liquid is poured with the vessel & as the level reaches h, the pressure of the liquid raises the vessel. The radius of the base of the vessel is R and half angle of the cone is  $\alpha$  and the weight of the vessel is W. What is the density of the liquid?



8. A cylindrical tank having cross-sectional area A = 0.5 m² is filled with two liquids of densities  $\rho_1$  = 900 kgm<sup>-3</sup> &  $\rho_2$ =600 kgm<sup>-3</sup>, to a height h = 60 cm as shown in the figure. A small hole having area a = 5 cm² is made in right vertical wall at a height y = 20 cm from the bottom. Calculate



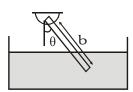
- (i) velocity of efflux.
- (ii) horizontal force F to keep the cylinder in static equilibrium, if it is placed on a smooth horizontal plane
- (iii) Minimum and maximum value of F to keep the cylinder at rest. The coefficient of friction between cylinder and the plane is  $\mu=0.1$
- (iv) velocity of the top most layer of the liquid column and also the velocity of the boundary separating the two liquids.
- 9. A cylindrical wooden float whose base area  $S=4000~cm^2$  & the altitude H=50~cm drifts on the water surface. Specific weight of wood  $d=0.8~gf/cm^3$ .
  - (i) What work must be performed to take the float out of the water?
  - (ii) Compute the work to be performed to submerged completely the float into the water.
- **10**. A cylindrical rod of length  $\ell$  = 2m & density  $\frac{\rho}{2}$  floats vertically in a liquid of density  $\rho$  as shown in figure.



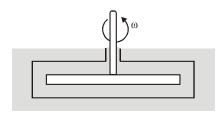
- (i) Show that it performs SHM when pulled slightly up & released & find its time period. Neglect change in liquid level.
- (ii) Find the time taken by the rod to completely immerse when released from position shown in (b). Assume that it remains vertical throughout its motion. (take  $g=\pi^2$  m/s<sup>2</sup>)



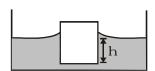
A uniform rod of length b capable of turning about its end which is out of water, rests inclined to the vertical. If its specific gravity is 5/9, find the length immersed in water.



- On the opposite sides of a wide vertical vessel filled with water two identical holes are opened, each having 12. the cross-sectional area S = 0.50 cm<sup>2</sup>. The height difference between them is equal to Dh = 51 cm. Find the resultant force of reaction of the water flowing out of the vessel.
- A thin horizontal disc of radius R = 10 cm is located with in a cylindrical cavity filled with oil whose viscosity  $\eta$  = 0.08 P (figure). The distance between the disc and the horizontal planes of the cavity is equal to h = 1.0 mm. Find the power developed by the viscous forces acting on the disc when it rotates with the angular velocity  $\omega$ =60 rad/s. The end effects are to be neglected.



A cube with a mass 'm' completely wettable by water floats on the surface of water. Each side of the cube is 'a'. What is the distance h between the lower face of cube and the surface of the water if surface tension is S. Take density of water as  $\rho_w$ . Take angle of contact is zero.



When a vertical capillary of length  $\ell$  with the sealed upper end was brought in contact with the surface of a liquid, the level of this liquid rise to the height h. The liquid density is p, the inside diameter of the capillary is d, the contact angle is  $\theta$ , the atmospheric pressure is  $P_0$ . Find the surface tension of the liquid.

# BRAIN STORMING SUBJECTIVE EXERCISE

# ANSWER KEY

EXERCISE-4(B)

1. 5 cm

- **2**. (i)  $t_2 = t_1 \left| \frac{d_L}{dL d} \right|$  (ii) No (iii) does not depend
- $\textbf{3.} \ \, \text{(i)} \ \, \text{(a)} \ \, D = \frac{5}{4} \, \, \text{d} \ \, \text{(b)} \quad P = P_{_0} \, + \, \, \frac{1}{4} \quad \text{(6H+L)} \ \, \text{dg (ii)} \ \, \text{(a)} \ \, v \, = \, \, \sqrt{\frac{g}{2} \big( 3H 4h \big)} \quad \text{(b)} \ \, x \, = \, \, \sqrt{h \big( 3H 4h \big)} \quad \text{(c)} \ \, x_{_{max}} \, = \, \frac{3}{4} \quad H = \frac{3}{4} \, \, \text{(b)} \, \, \text{(b)} \, \, x \, = \, \, \sqrt{h \left( 3H 4h \right)} \, \, \, \text{(c)} \, \, x_{_{max}} \, = \, \frac{3}{4} \, \, H = \frac{$
- 4. 6N

- $\boldsymbol{5}.$  (i)  $4\text{m/s}^2$  (ii) 10% (iii) 0,~45~kPa

- 7.  $\rho = \frac{w}{\pi h^2 g \tan \alpha \left( R \frac{1}{2} h \tan \alpha \right)}$  8. (i) 4 m/s (ii) F = 7.2 N (iii)  $F_{min} = 0$ ,  $F_{max} = 52.2$  N (iv) both 4 10<sup>-3</sup> m/s
- 9. (i)  $\frac{d^2H^2S}{2\rho g}$  = 32 kgf-m (ii)  $\frac{1}{2}$  SH<sup>2</sup> (1-d<sup>2</sup>) = 2Kgf-m 10. (i) 2 sec (ii) 1 sec

**12**. 0.50 N

- 14.  $h = \frac{mg + 4Sa}{\rho_w a^2 g}$  15.  $\left\lceil \rho g h + \frac{P_0 h}{\ell h} \right\rceil \frac{d}{4 \cos \theta}$

EX	ERCISE-05	(A)	PREVIO	US YEAR QUESTIONS
1.				weight of 200 N to the lower red in the wire is- [AIEEE - 2003] (4) 0.1 J
2.	A wire fixed at the is-	e upper end stretches by len	gth $\ell$ by applying a force F	F. The work done in stretching [AIEEE - 2004]
	$(1) \ \frac{F}{2\ell}$	(2) Fℓ	(3) 2Fℓ	$(4) \frac{F\ell}{2}$
3.	If S is stress and Y is-	' is Young's modulus of mater	rial of a wire, the energy sto	red in the wire per unit volume
	(1) 2S <sup>2</sup> Y	(2) $\frac{S^2}{2Y}$	$(3) \frac{2Y}{S^2}$	$(4) \frac{S}{2Y}$
4.		$g$ $\ell$ mm when a load W is hat the two ends, the elongat (2) $2\ell$	_	s over a pulley and two weights mm)- [AIEEE - 2006] (4) $\ell/2$
5.	-	nt 20 m is completely filled w e side wall of the cylinder n (2) 20		flux of water (in ms <sup>-1</sup> ) through [AIEEE - 2002] (4) 5
6.	force acting on the (1) directly propor (2) directly propor (3) inversely propor		portional to v velocity v velocity v	velocity v. the retarding viscous [AIEEE - 2004]
7.	<ul><li>(1) air flows from</li><li>(2) air flows from</li></ul>	es of different radii are conn the bigger bubble to the sm bigger bubble to the smaller the smaller bubble to the bi w of air	aller bubble till the sizes be bubble till the sizes are int	
8.		illary tube is dipped in wate ing elevator, the length of w (2) 10 cm	<del>-</del>	m. If the entire arrangement is tube will be- [AIEEE - 2005]  (4) 20 cm
0	Tf 41 4 1 1	1 ( 1 ( 1 ( 1 ( 1 ( 1 ( 1 ( 1 ( 1 ( 1 (	-:	/

If the terminal speed of a sphere of gold (density =  $19.5 \text{ kg/m}^3$ ) is 0.2 m/s in a viscous liquid (density =  $1.5~kg/m^3$ ), find the terminal speed of a sphere of silver (density= $10.5~kg/m^3$ ) of the same size in the same liquid. (2) 0.133 m/s(3) 0.1 m/s(4) 0.2 m/s(1) 0.4 m/s

A spherical solid ball of volume V is made of a material of density  $\rho_1$ . It is falling through a liquid of density  $\rho_2(\rho_2 < \rho_1)$ . Assume that the liquid applies a viscous force on the ball that is propoertional to the square of its speed v, i.e.,  $\boldsymbol{F}_{_{viscous}}$  =  $-kv^2$  (k > 0). Then terminal speed of the ball is [AIEEE - 2008]

 $(1) \sqrt{\frac{Vg(\rho_1 - \rho_2)}{k}}$ 

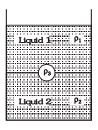
 $(2) \frac{Vg\rho_1}{k}$ 

(3)  $\sqrt{\frac{Vg\rho_1}{k}}$ 

 $(4) \ \frac{Vg\left(\rho_1-\rho_2\right)}{k}$ 

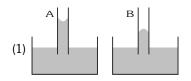


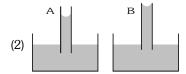
A jar is filled with two non-mixing liqudis 1 and 2 having densities  $\rho_1$  and  $\rho_2$ , respectively. A solid ball, made of a material of density  $\rho_3$ , is dropped in the jar. It comes to equilibrium in the position shown in the figure. Which of the following is true for  $\,\rho_1\,$  ,  $\,\rho_2\,$  and  $\,\rho_3\,$ [AIEEE - 2008]

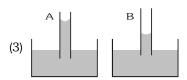


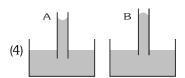
- (1)  $\rho_3 < \rho_1 < \rho_2$
- (2)  $\rho_1 > \rho_3 > \rho_2$

- (3)  $\rho_1 < \rho_2 < \rho_3$  (4)  $\rho_1 < \rho_3 < \rho_2$
- 12. A capillary tube (1) is dipped in water. Another identical tube (2) is dipped in a soap -water solution. Which of the following shows the relative nature of the liquid columns in the two tubes? [AIEEE - 2008]









- A spherical solid ball of volume V is made of a material of density  $\rho_1$ . It is falling through a liquid of density  $\rho_2$  $(\rho_2 < \rho_1)$ . Assume that the liquid applies a viscous force on the ball that is proportional to the square of its speed v. i.e.,  $F_{viscous} = -kr^2$ , k > 0. The terminal speed of the ball is -[AIEEE-2008]
  - $(1) \sqrt{\frac{Vg(\rho_1 \rho_2)}{I_2}}$
- (2)  $\frac{Vg\rho_1}{k}$
- (3)  $\sqrt{\frac{Vg\rho_1}{I_r}}$
- $(4) \frac{V(\rho_1 \rho_2)}{k}$
- Two wires are made of the same material and have the same volume. However wire 1 has cross-sectional area A and wire 2 has cross-sectional area 3A. If the length of wire 1 increases by  $\Delta x$  on applying force F, how much force is needed to stretch wire 2 by the same amount? [AIEEE-2009] (1) 6F (2) 9F (3) F (4) 4F
- A ball is made of a material of density  $\rho$  where  $\rho_{\text{oil}} \leq \rho \leq \rho_{\text{water}}$  with  $\rho_{\text{oil}}$  and  $\rho_{\text{water}}$  representing the densities of oil and water, respectively. The oil and water are immiscible. If the above ball is in equilibrium in a mixture of this oil and water, which of the following pictures represents its equilibrium position? [AIEEE-2010]









Water is flowing continuously from a tap having an internal diameter  $8 ext{10}^{-3}$  m. The water velocity as it leaves the tap is  $0.4 \text{ ms}^{-1}$ . The diameter of the water stream at a distance  $2 \cdot 10^{-1} \text{ m}$  below the tap is close to :-

[AIEEE-2011]

- $(1) 9.6 10^{-3} m$
- (2) 3.610-3 m
- (3)  $5.0 10^{-3} m$
- (4)  $7.5 10^{-3} m$



- 17. Work done in increasing the size of a soap bubble from a radius of 3 cm to 5cm is nearly (Surface tension of soap solution =  $0.03 \text{ Nm}^{-1}$ ):-
  - (1)  $2\pi$  mJ
- (2)  $0.4 \pi \text{ mJ}$
- (3)  $4\pi$  mJ
- (4)  $0.2 \pi \text{ mJ}$
- 18. Two merucry drops (each of radius 'r') merge to form a bigger drop. The surface energy of the bigger drop, ifs T is the surface tension, is:
  - (1)  $2^{\frac{5}{3}} \pi r^2 T$
- (2)  $4\pi r^2 T$

(3)  $2\pi r^2 T$ 

- (4)  $2^{8/3} \pi r^2 T$
- 19. If a ball of steel (density  $\rho$  = 7.8 g cm<sup>-3</sup>) attains a terminal velocity of 10 cm s<sup>-1</sup> when falling in a tank of water (coefficient of viscosity  $\eta_{water}$  = 8.5  $10^{-4}$  Pa.s) then its terminal velocity in glycerine ( $\rho$  = 12 g cm<sup>-3</sup>,  $\eta$  = 13.2 Pa.s) would be nearly :-
  - (1)  $1.6 10^{-5} cm s^{-1}$
- (2)  $6.25 10^{-4} cm s^{-1}$
- (3)  $6.45 10^{-4} cm s^{-1}$
- (4)  $1.5 10^{-5} cm s^{-1}$
- 20. A thin liquid film formed between a U-shaped wire and a light slider supports a weight of  $1.5 ext{ } 10^{-2} ext{ N}$  (see figure). The length of the slider is 30 cm and its weight negligible. The surface tension of the liquid film is:-



(1) 0.025 Nm<sup>-1</sup>

- (2) 0.0125 Nm<sup>-1</sup>
- (3) 0.1 Nm<sup>-1</sup>
- (4) 0.05 Nm<sup>-1</sup>

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Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	
Ans.	4	4	2	1	2	2	3	4	3	1	4	3	1	2	3	2	2	4	2	1	

# PREVIOUS YEAR QUESTIONS

# MCQ'S (only one correct answers)

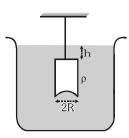
- 1. Water from a tap emerges vertically downwards with an initial speed of 1.0 m/s. The cross-sectional area of tap is  $10^{-4} \text{ m}^2$ . Assume that the pressure is constant throughout the stream of water and that the flow is steady, the cross-sectional area of stream 0.15 m below the tap is :- [IIT-JEE 1998]
  - (A)  $5.0 10^{-4} m^2$
- (B)  $1.0 10^{-4} m^2$
- (C)  $5.0 10^{-5} m^2$
- (D)  $2.0 10^{-5} m^2$
- 2. A given quantity of an ideal gas is at pressure P and absolute temperature T. The isothermal bulk modulus of the gas is :-
  - (A) 2/3 P

(B) P

- (C) 3/2 P
- (D) 2P
- 3. A closed compartment containing gas is moving with some acceleration in horizontal direction. Neglect effect of gravity. Then, the pressure in the compartment is:-
  - (A) same every where
- (B) lower in front side
- (C) lower in rear side
- (D) lower in upper side
- 4. A large open tank has two holes in the wall. One is a square hole of side L at a depth y from the top and the other is a circular hole of radius R at a depth 4y from the top. When the tank is completely filled with water, the quantities of water flowing out per second from the holes are both same. Then, R is equal to :-
  - (A)  $\frac{L}{\sqrt{2\pi}}$

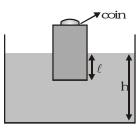
- (B) 2πL
- (C) L

- (D)  $\frac{L}{2\pi}$
- 5. A hemispherical portion of radius R is removed from the bottom of a cylinder of radius R. The volume of the remaining cylinder is V and mass M. It is suspended by a string in a liquid of density  $\rho$ , where it stays vertical. The upper surface of the cylinder is at a depth h below the liquid surface. The force on the bottom of the cylinder by the liquid is:
  [IIT-JEE 2001]



(A) Mg

- (B) Mg Vpg
- (C) Mg +  $\pi R^2 h \rho g$
- (D)  $\rho g (V + \pi R^2 h)$
- 6. A wooden block, with a coin placed on its top, floats in water as shown in figure. The distance  $\ell$  and h are shown there. After sometime the coin falls into the water. Then :- [IIT-JEE 2002]



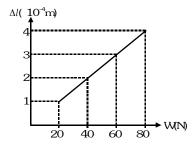
(A)  $\ell$  decreases and h increases

(B)  $\ell$  increases and h decreases

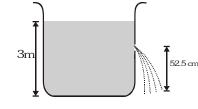
(C) both  $\ell$  and h increase

(D) both  $\ell$  and h decrease

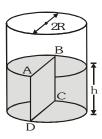
7. The adjacent graph shows the extension  $(\Delta \ell)$  of a wire of length 1m suspended from the top of a roof at one end and with a load W connected to the other end. If the cross-sectional area of the wire is  $10^{-6}$ m<sup>2</sup>, calculate the Young's modulus of the material of the wire :-IIIT-JEE 20031



- $10^{11} \text{ N/m}^2$ (A) 2
- $10^{-11} \text{ N/m}^2$ (B) 2
- $10^{12} \text{ N/m}^2$ (C) 3
- $10^{13} \text{ N/m}^2$ (D) 2
- 8. The pressure of a medium is changed from  $1.01 ext{ } 10^5 ext{ Pa}$  to  $1.165 ext{ } 10^5 ext{ Pa}$  and change in volume is 10% keeping temperature constant. The bulk modulus of the medium is :-[IIT-JEE 2005]
  - (A) 204.8 10<sup>5</sup> Pa
- (B) 102.4 10<sup>5</sup> Pa
- (C)  $51.2 10^5 Pa$
- 10<sup>5</sup> Pa (D) 1.55
- 9. Water is filled in a cylindrical container to a height of 3 m. The ratio of the cross-sectional area of the orifice and the beaker is 0.1. The square of the speed of the liquid coming out from the orifice is  $(g = 10 \text{ m/s}^2)$

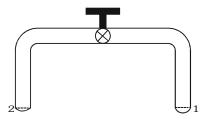


- (A)  $50 \text{ m}^2\text{s}^2$
- (B)  $50.5 \text{ m}^2\text{s}^2$
- (C) 51 m<sup>2</sup>s<sup>2</sup>
- (D)  $52 \text{ m}^2\text{s}^2$
- Water is filled up to a height h in a beaker of radius R as shown in the figure. The density of water is  $\rho$ , the surface tension of water is T and the atmospheric pressure is  $P_0$ . Consider a vertical section ABCD of the water column through a diameter of the beaker. The force on water on one side of this section by water on the other side of this section has magnitude :-[IIT-JEE 2007]



- (A)  $[2P_0Rh + \pi R^2 \rho gh 2RT]$
- (C)  $[P_0\pi R^2 + R\rho gh^2 2RT]$

- (B)  $[2P_{0}Rh + R\rho gh^{2} 2RT]$ (D)  $[P_{0}\pi R^{2} + R\rho gh^{2} + 2RT]$
- A glass tube of uniform internal radius (r) has a valve separating the two identical ends. Initially, the valve is in a tightly closed position. End 1 has a hemispherical soap bubble of radius r. End 2 has sub-hemispherical soap bubble as shown in figure. Just after opening the valve, [IIT-JEE 2008]





- (A) Air from end 1 flows towards end 2. No change in the volume of the soap bubbles.
- (B) Air from end 1 flows towards end 2. Volume of the soap bubble at end 1 decreases.
- (C) No change occurs
- (D) Air from end 2 flows towards end 1. Volume of the soap bubble at end 1 increases.
- One end of a horizontal thick copper wire of length 2L and radius 2R is welded to an end of another horizontal thin copper wire of length L and radius R. When the arrangement is stretched by applying forces at two ends, the ratio of the elongation in the thin wire to that in the thick wire is :-
  - (A) 0.25
- (B) 0.50
- (C) 2.00
- (D) 4.00

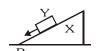
# MCQ'S (Multiple Correct answers)

- 1. A solid sphere of radius R and density p is attached to one end of a mass-less spring of force constant k. The other end of the spring is connected to another solid sphere of radius R and density 3p. The complete arrangement is placed in a liquid of density 2p and is allowed to reach equilibrium. The correct statement(s) is (are)
  - (A) the net elongation of the spring is  $\frac{4\pi R^3 \rho g}{3k}$  (B) the net elongation of the spring is  $\frac{8\pi R^3 \rho g}{3k}$
  - (C) the light sphere is partially submerged.
- (D) the light sphere is completely submerged.

# Match the Column Type

1. Column II shows five systems in which two objects are labelled as X and Y. Also in each case a point P is shown. Column I gives some statements about X and/or Y. Match these statements to the appropriates system (s) from Column II. IIIT-JEE 20091

Column I



Column II

Block Y of mass M left on a fixed inclined plane X, Slides on it with a constant velocity.

The gravitational potential (q) kept energy of X is continuously increasing.

(A) The forces exerted by X on

Y has a magnitude Mg



Two ring magnets Y and Z, each of mass M are in frictionless vertical plastic stand so that they repel each other. Y rests on the base X and Z hangs in air in equilibrium. P is the topmost point of the stand on the common axis of the two rings. The whole system is in a lift that is going up with a constant velocity.

(C) Mechanical energy of the system X + Y is continuously decreasing.



(r)

A pulley Y of mass mo is fixed to a table through a clamp X. A block of mass M hangs from a string that goes over the pulley and is fixed at point P of the table. The whole system is kept in a lift that is going down with a constant velocity.

The torque of the weight of 'Y' about point P is zero



A sphere Y of mass M is put in a non viscous liquid X kept in a container at rest. The sphere is released and it moves down in the liquid.



A sphere Y of mass M is falling with its terminal velocity in a viscous liquid X kept in a container

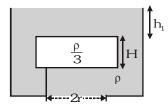


#### Comprehension Based Question

# Comprehension#1

A wooden cylinder of diameter 4r, height H and density  $\rho/3$  is kept on a hole of diameter 2r of a tank, filled with liquid of density  $\rho$  as shown in the figure.

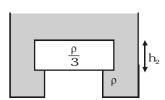
1. Now level of the liquid starts decreasing slowly. When the level of liquid is at a height  $h_1$  above the cylinder the block starts moving up. At what value of  $h_1$ , will the block rise :- [IIT-JEE 2006]



(A)  $\frac{4h}{9}$ 

(B)  $\frac{5h}{9}$ 

- (C)  $\frac{5h}{3}$
- (D) remains same
- 2. The block in the above question is maintained at the position by external means and the level of liquid is lowered. The height h<sub>2</sub> when this external force reduces to zero is :- [IIT-JEE 2006]



(A)  $\frac{4h}{9}$ 

(B)  $\frac{5h}{9}$ 

- (C) remains same (D)  $\frac{2h}{3}$
- 3. If height  $h_2$  of water level is further decreased, then :-

[IIT-JEE 2006]

- (A) cylinder will not move up and remains at its original position
- (B) for  $h_2 = h/3$ , cylinder again starts moving up
- (C) for  $h_2 = h/4$ , cylinder again starts moving up
- (D) for  $h_2 = h/5$  cylinder again starts moving up

#### Assertion-Reason

1. Statement-1: The stream of water flowing at high speed from a garden hose pipe tends to spread like a fountain when held vertically up, but tends to narrow down when held vertically down. [IIT-JEE 2008]

and

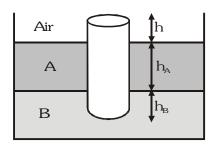
Statement-2: In any steady flow of an incompressible fluid, the volume flow rate of the fluid remains constant.

- (A) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
- (B)Statement-1 is True, Statement-2 is True; Statement-2 is not a correct explanation for Statement-1
- (C) Statement-1 is True, Statement-2 is False
- (D) Statement-1 is False, Statement-2 is True



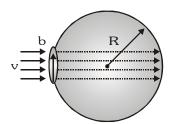
#### Subjective Type Questions

- 1. A wooden stick of length L, radius R and density  $\rho$  has a small metal piece of mass m (of negligible volume) attached to its one end. Find the minimum value for the mass m (in terms of given parameters) that would make the stick float vertically in equilibrium in a liquid of density  $\sigma$  (>  $\rho$ ). [IIT-JEE 1999]
- 2. A uniform solid cylinder of density  $0.8~g/cm^3$  floats in equilibrium in a combination of two non-mixing liquids A and B with its axis vertical. The densities of the liquids A and B are  $0.7~g/cm^3$  and  $1.2~g/cm^3$ , respectively. The height of liquid A is  $h_A = 1.2~cm$ . The length of the part of the cylinder immersed in liquid B is  $h_B = 0.8~cm$ .



- (i) Find the total force exerted by liquid A on the cylinder.
- (ii) Find h, the length of the part of the cylinder in air.
- (iii) The cylinder is depressed in such a way that its top surface is just below the upper surface of liquid A and is then released. Find the acceleration of the cylinder immediately after it is released.
- 3. A bubble having surface tension T and radius R is formed on a ring of radius R b (b<<R). Air is blown inside the tube with velocity R0 as shown. The air molecule collides perpendicularly with the wall of the bubble and stops. Calculate the radius at which the bubble separates from the ring.

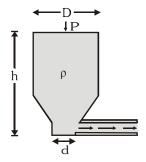
  [IIT-JEE 2003]



**4.** Shown in the figure is a container whose top and bottom diameters are D and d respectively. At the bottom of the container, thee is a capillary tube of outer radius b and inner radius a. The volume flow rate in the capillary is Q. If the capillary is removed the liquid comes out with a velocity of  $v_0$ . The density of the liquid

is given as calculate the coefficient of viscosity  $\eta$ . (Given :  $\pi a^2 = 10^{-6} \text{ m}^2$  and  $\frac{a^2}{l} = 2 10^{-6} \text{ m}$ )

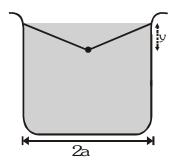
[IIT-JEE 2003]





5. A container of width 2a is filled with a liquid. A thin wire of weight per unit length  $\lambda$  is gently placed over the liquid surface in the middle of the surface as shown in the figure. As a result, the liquid surface is depressed by a distance y (y << a). Determine the surface tension of the liquid.

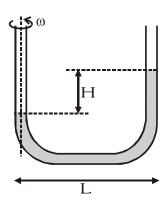
[IIT-JEE 2004]



6. Consider a horizontally oriented syringe containing water located at a height of 1.25 m above the ground. The diameter of the plunger is 8 mm and the diameter of the nozzle is 2 mm. The plunger is pushed with a constant speed of 0.25 m/s. Find the horizontal range of water stream on the ground. (Assume liquid is compressible and non-viscous) (Take g = 10 m/s<sup>2</sup>). [IIT-JEE 2004]



7. A U-shaped tube contains a liquid of density  $\rho$  and it is rotated about the line as shown in the figure. Find the difference in the levels of liquid column. [IIT-JEE 2005]



### Integer Type Questions

1. Two soap bubbles A and B are kept in a closed chamber where the air is maintained at pressure  $8 \text{ N/m}^2$ . The radii of bubbles A and B are 2 cm and 4 cm, respectively. Surface tension of the soap-water used to make bubbles is 0.04 N/m. Find the ratio  $n_B/n_A$ , where  $n_A$  and  $n_B$  are the number of moles of air in bubbles A and B, respectively. [Neglect the effect of gravity] :-



2. A cylindrical vessel of height 500 mm has an orifice (small hole) at its bottom. The orifice is initially closed and water is filled in it up to height H. Now the top is completely sealed with a cap and the orifice at the bottom is opened. Some water comes out from the orifice and the water level in the vessel becomes steady with height of water column being 200 mm. Find the fall in height (in mm) of water level due to opening of the orifice. [Take atmospheric pressure =  $1.0 10^5 N.m^2$ , density of water =  $1000 kg/m^3$  and g=10 m/s<sup>2</sup>. Neglect any effect of surface tension.] [IIT-JEE 2009]

PREVIOUS YEARS QUESTIONS	ANSWER	KEY		EXERCISE	-5
• MCQ's (Single Correct answers)		<b>8</b> . D	<b>4</b> . A <b>10</b> . B	<b>6</b> . D	

- MCQ's (Multiple Correct answers) **1.** (A, D)
- Match the Column Type **1.** (A) p,t (B) q,s,t (C) p,r,t (D) q
- **2**. A Comprehension Based Questions **1**. C
- 1. A Assertion-Reason
- 1.  $\pi R^2 L(\sqrt{\rho \sigma} \rho)$  2. (i) zero (ii) 0.25 m (iii)  $\frac{g}{6}$  3.  $R = \frac{4T}{\rho v^2}$

Subjective Questions 1. 
$$\pi R^2 L(\sqrt{\rho \sigma - \rho})$$
 2. (i) zero (ii) 0.25 m (iii)  $\frac{s}{6}$  3.  $R = \frac{s}{\rho v}$ 

**4**. 
$$\eta = \frac{\pi}{8Q\ell} \times \frac{1}{2} \rho v_0^2 \left[ 1 - \left( \frac{A_2}{A_1} \right)^2 \right] \times a^4$$
 where  $\frac{A_2}{A_1} = \frac{b^2}{D^2}$ 

**3**. A

**5**. 
$$\frac{\lambda a}{2y}$$
 **6**. 2m **7**. H=  $\frac{\omega^2 L^2}{2g}$ 

Integer Type Questions 1. 6 **2**. 206